



University at Buffalo

The State University of New York

Lecture #3c

Effects of Fines on Liquefaction Resistance & CPT Resistance

S. Thevanayagam

Associate Professor

Department of Civil Structural & Environmental Engineering

Director of Education, MCEER

University at Buffalo, NY, USA

Acknowledgments:

J. Liang, T. Shenthana, T. Kanagalingam, N. Ecmis; NSF, USGS NEHRP, MCEER, FHWA

Workshop on Earthquakes and Soil Liquefaction, Griffith University, Australia, December 14, 2007

Organized by Prof. A. Balasubramaniam

PROBLEM

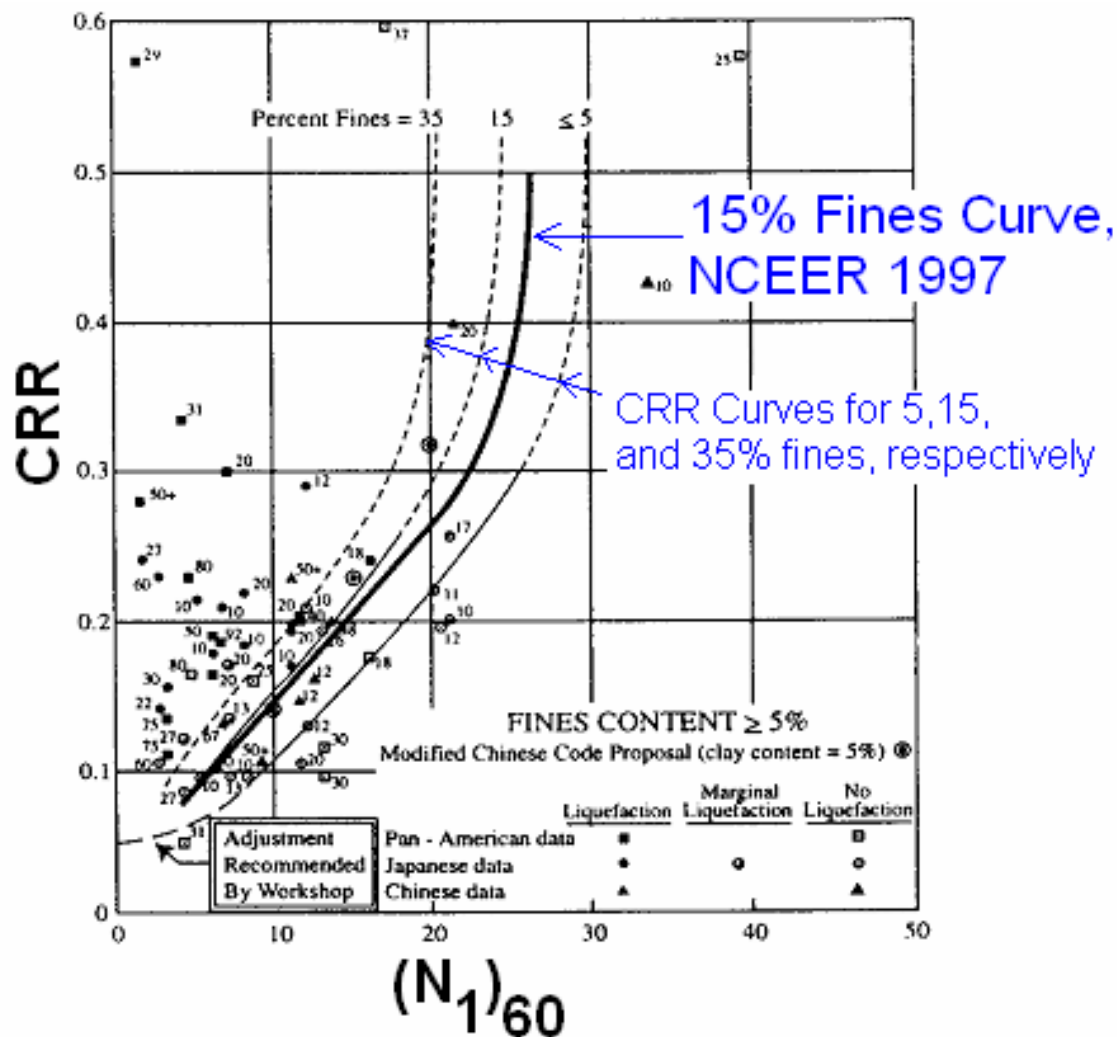
- Many earthquake-induced liquefaction and lateral spreading have occurred in silty soil sites. There is a need to understand Liquefaction Behavior of Silty Soils as compared to Clean Sands.
- Current Liquefaction Screening Technique for sands and non-plastic silty soils is highly empirical
 - Current empirical charts are based on field observation from sand and silty sand sites and data on clean sands (NCEER 1997).
 - The rationale for these methods for silty soils is not fully understood
 - High uncertainty in these methods

Current Liquefaction Screening Methods

Method	Resistance ($CRR_{7.5}$)	x	Factor of Safety
SPT $(N_1)_{60}$	$[a+cx+ex^2+gx^3]/[1+bx+d x^2+fx^3+hx^4]$	$(N_1)_{60CS}$ $=\alpha + \beta$ $(N_1)_{60}$	
CPT q_{c1N}	$0.833[x/1000]+0.05$ for $x<50$ $93[x/1000]^3+0.08$ for $50<x<160$	$(q_{c1N})_{CS}$ $K_c \bar{q}_{c1N}$	$(CRR_{7.5}/CSR)MSF$
S-wave V_{s1}	$r(V_{s1}/100)^2 + s[1/(V_{s1c}-V_{s1})-1/V_{s1c}]$	V_{s1}	

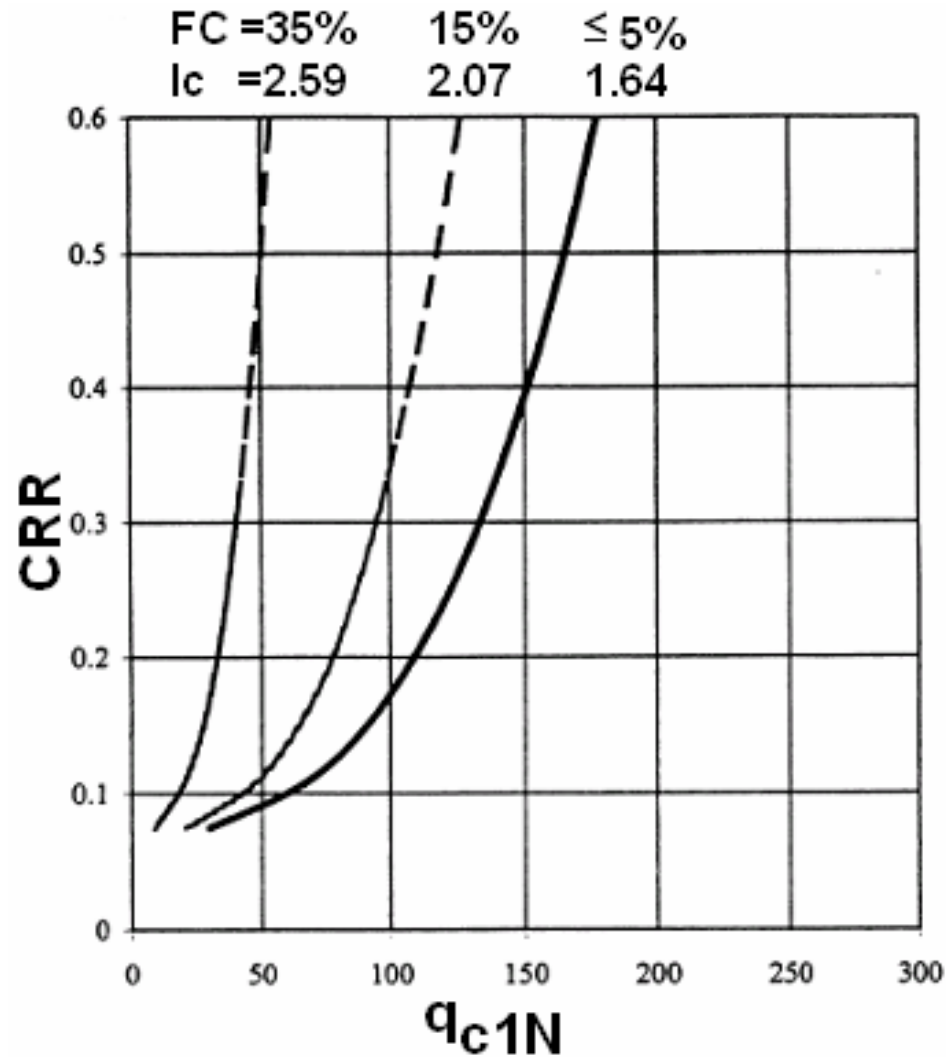
$\alpha, \beta, K_c, V_{s1c} = \text{silt content dependent}$

SPT Method



(Youd and Idriss, 2001)

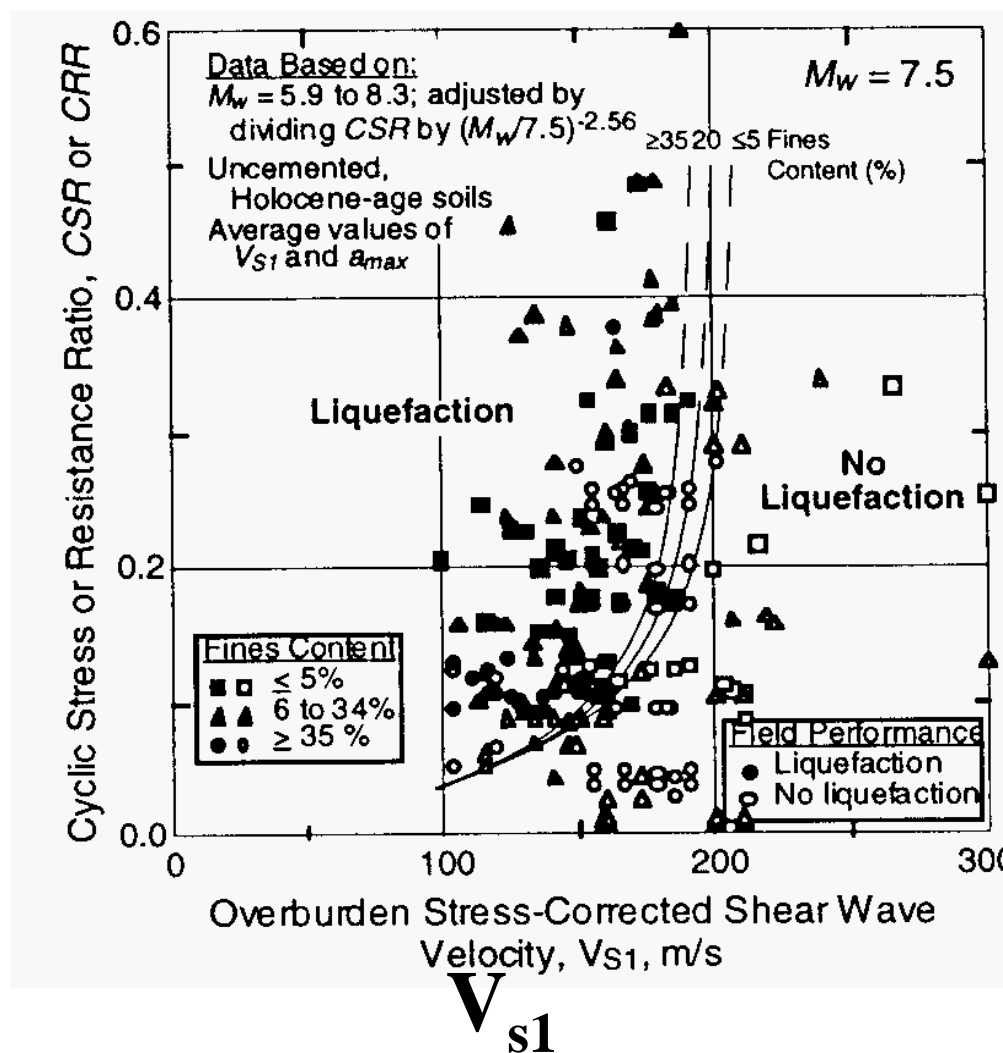
CPT Method



(Robertson and Wride, 1998)

S-Wave Method

CRR



(Andrus and Stokoe et al. 2000)

LIQUEFACTION SCREENING QUESTIONS

- Why SPT/CPT/ V_s charts
 - depend on silt content ?
 - not affected by silt content > 35% ?

- What Controls
 - Penetration Resistance - q_{c1N} and $(N_1)_{60}$?
 - Liquefaction Resistance – CRR ?

- How to account for effects of silt content on CRR – Penetration Resistance Relationships ?

OBJECTIVES

- Synthesize current knowledge, site observations, and experience in silty soils
- Understand and Contrast Liquefaction of Silty Soils and Sands
- Understand Factors Affecting Penetration Resistances
- Understand relationship between penetration resistance and liquefaction resistance
- Develop Advanced Methods and Guidelines for Liquefaction Screening

Outline

- Experimental Study
 - Effects of fines on Liquefaction Resistance
- Numerical study
 - to simulate cone penetration in a soil
 - to find the effect of hydraulic conductivity (k) and compressibility (m_v) on pore pressures and cone penetration resistance in soils
- Laminar box liquefaction experiments and cone penetration tests (CPT) on clean sands
- Develop Advanced Methods and Guidelines for Liquefaction Screening

WORKING HYPOTHESIS

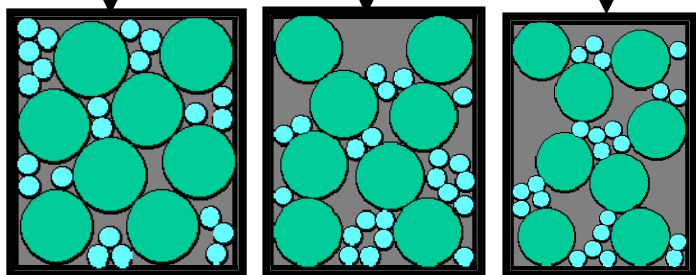
- Liquefaction resistance depends primarily on;
 - Inter-grain Contact Density
 - Contact density depends on e and fines content (FC)
- Permeability and compressibility depend on fines content, soil gradation, soil mineral
- Penetration Resistance depends primarily on;
 - Inter-grain Contact Density
 - C_v
 - Instrument Geometry
 - Penetration rate

MIX CLASSIFICATION

Inter Coarse Grain

$$FC < FC_{th}$$

Role of Fine Grain



$$e_c = (e + f_c) / (1 - f_c)$$

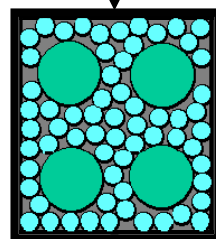
$$(e_c)_{eq} = (e + (1-b)f_c) / (1 - (1-b)f_c)$$

Inter Fine Grain

$$FC > FC_{th}$$

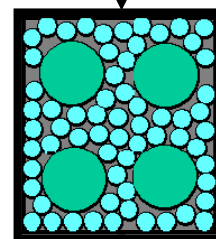
Role of Coarse Grain

$$FC > FC_L$$



$$e_f = e / f_c$$

$$FC_{th} < FC < FC_L$$



$$(e_f)_{eq} = e / (f_c + (1-f_c)/R_d^m)$$

Prime Contact

Sec. Contact

Microstructure

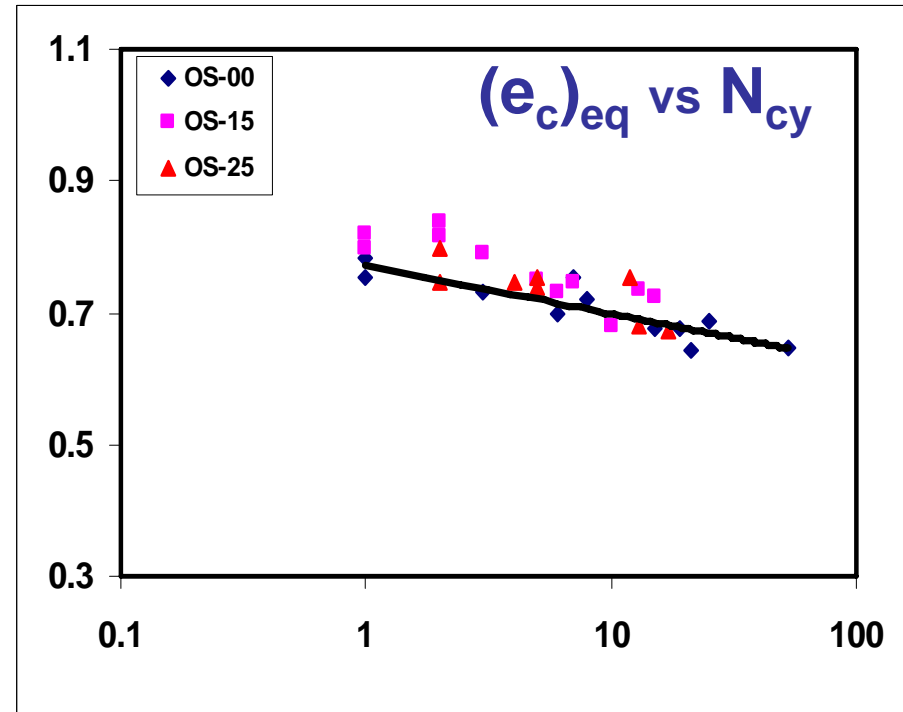
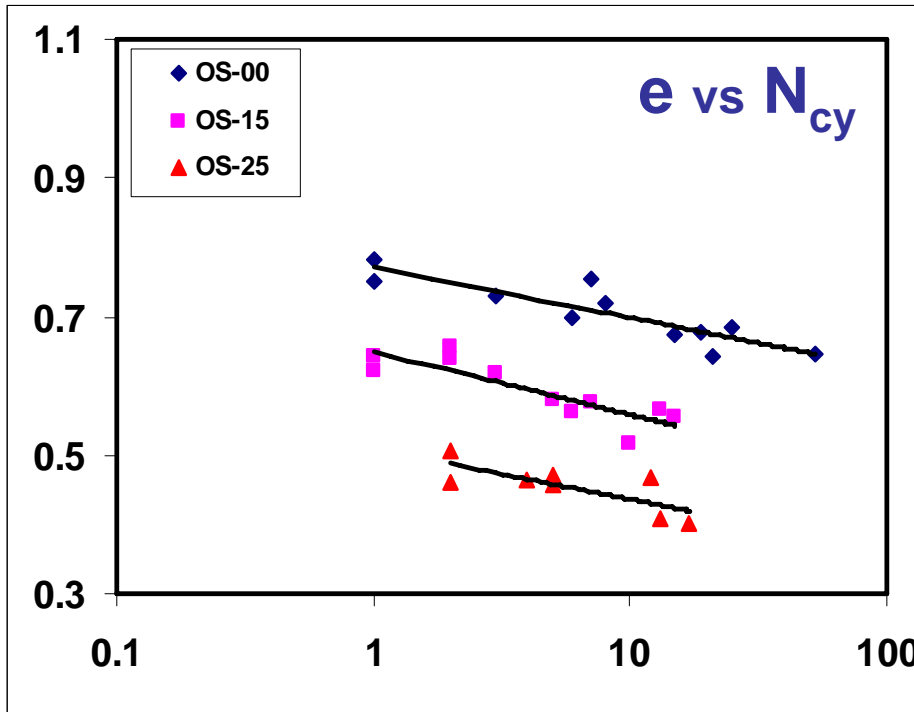
Contact Density
Index

WORKING HYPOTHESIS

- Liquefaction resistance depends primarily on;
 - Inter-grain Contact Density
 - Contact density depends on e and fines content (FC)
- Permeability and compressibility depend on fines content, soil gradation, soil mineral
- Penetration Resistance depends primarily on;
 - Inter-grain Contact Density
 - C_v
 - Instrument Geometry
 - Penetration rate

Effect of Fines Content on Cyclic Shear Strength

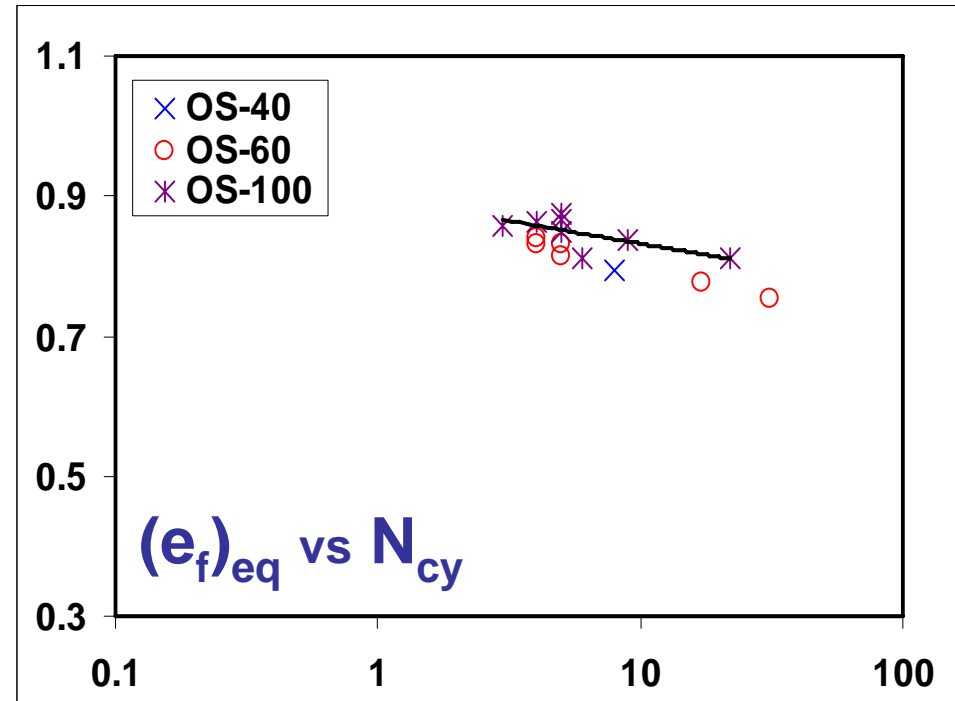
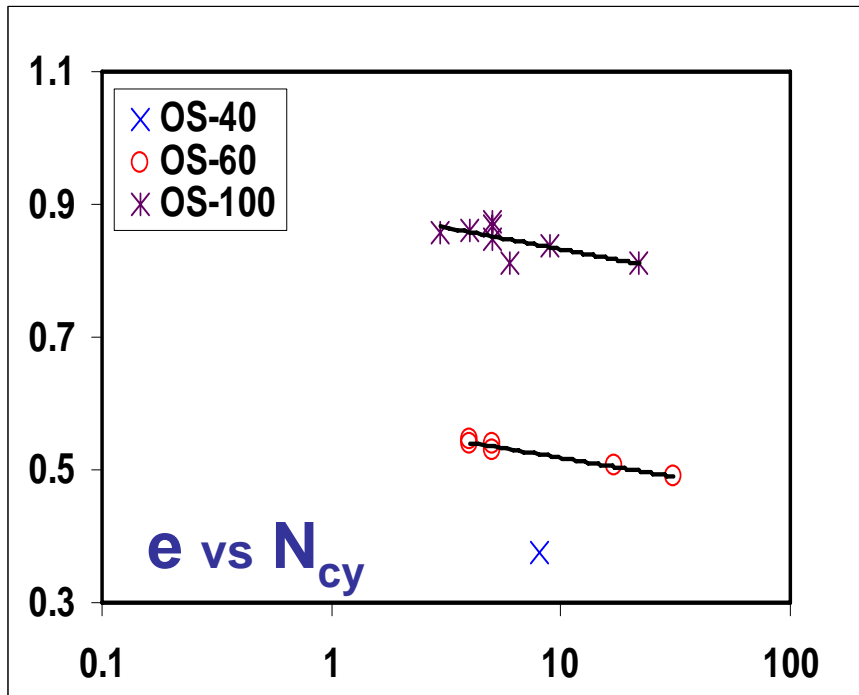
Silt Content < 25%



$(e_c)_{eq}$ correlates with N_{cy}
(Thevanayagam et al. 1999, 2001)

Effect of Fines Content on Cyclic Shear Strength

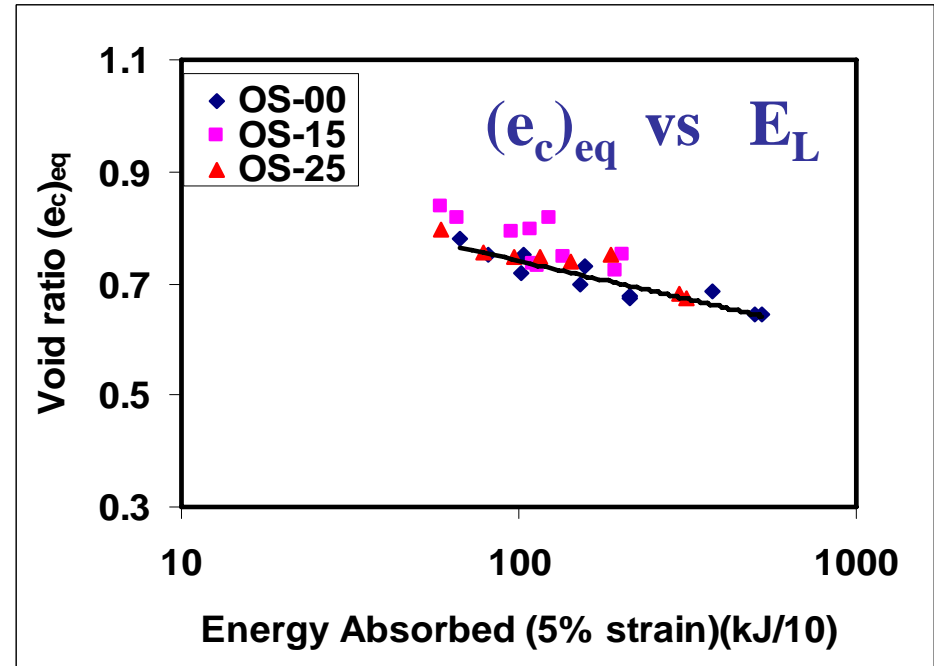
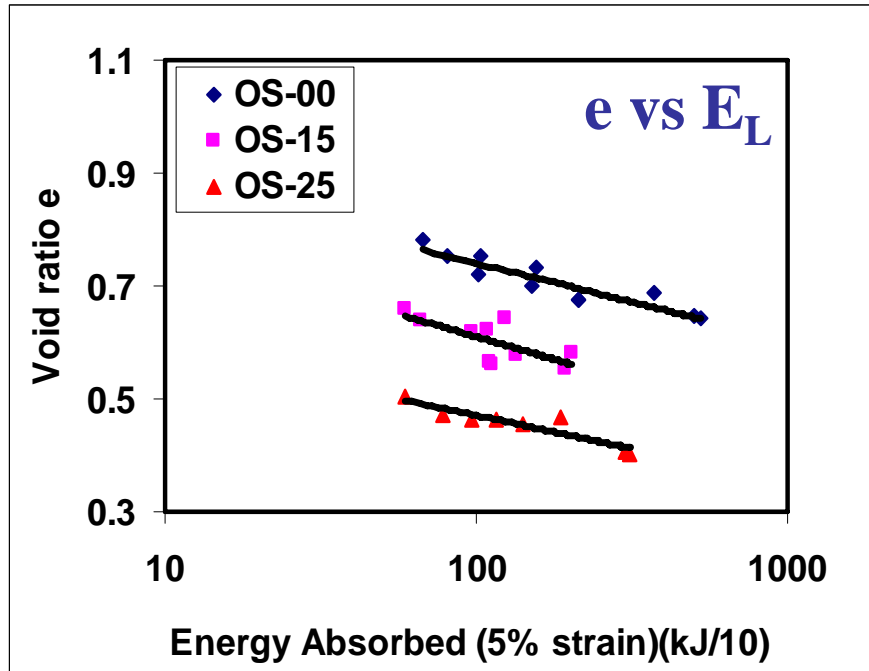
Silt Content > 25%



$(e_f)_{eq}$ correlates with N_{cy}
(Thevanayagam et al. 1999, 2001)

Effect of Fines Content on Strain-Energy

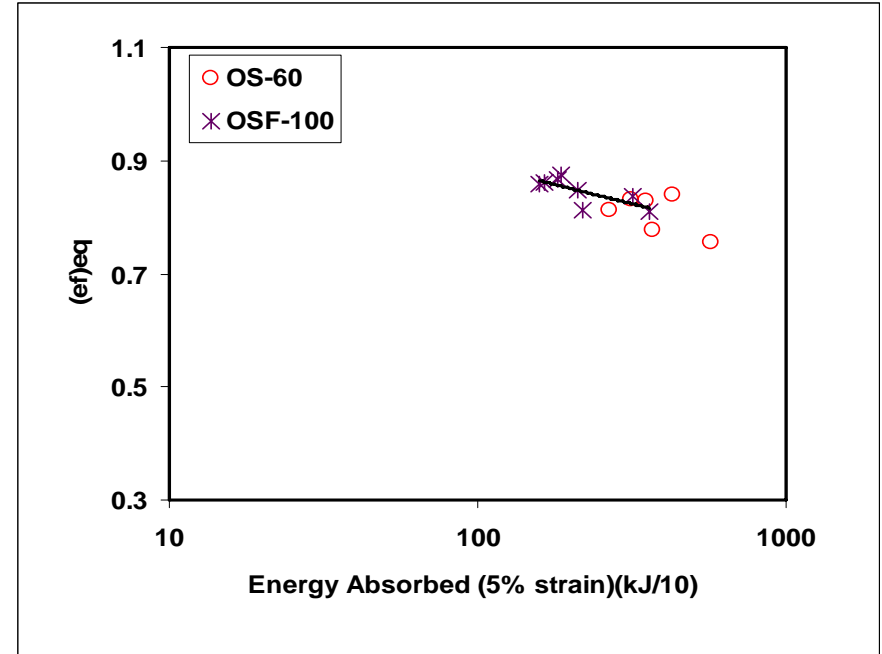
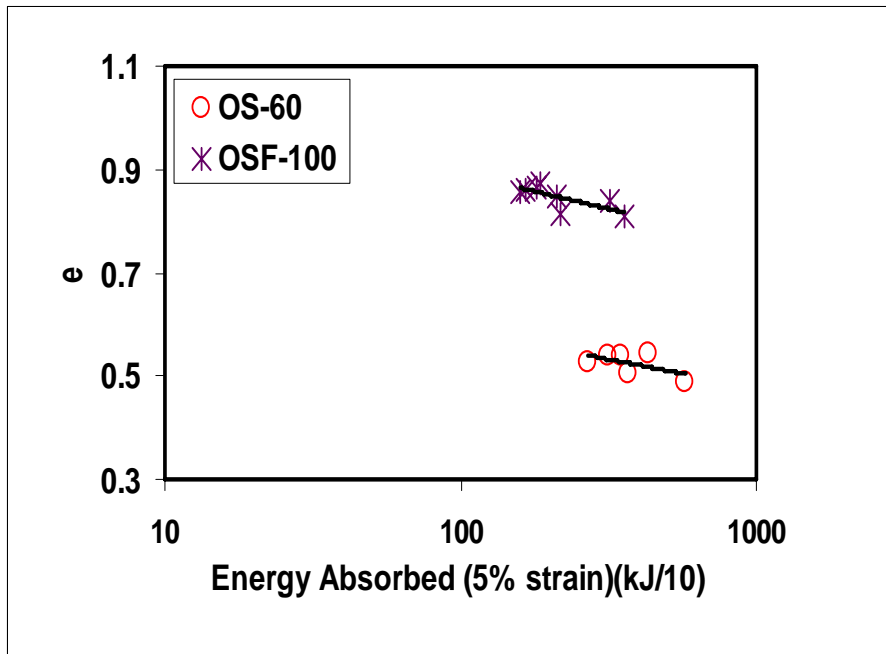
Silt Content < 25%



$(e_c)_{eq}$ correlates with E_L
(Thevanayagam et al. 2003)

Effect of Fines Content on Strain-Energy

Silt Content > 25%

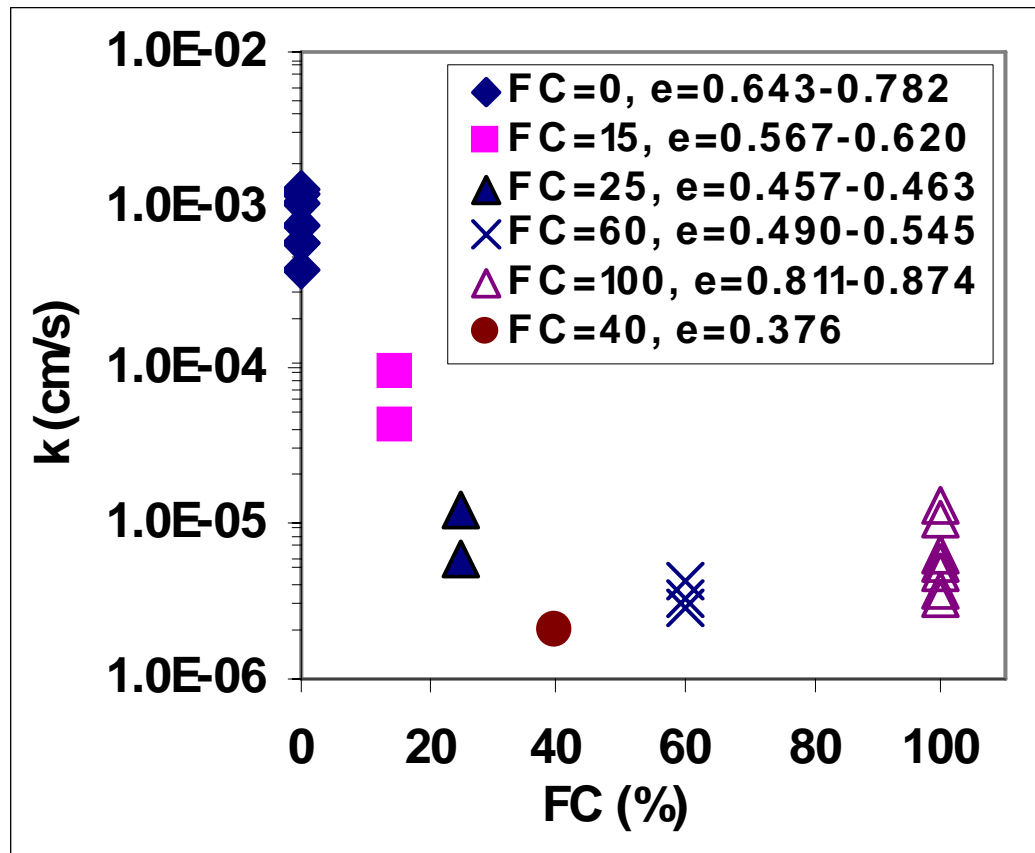


$(e_f)_{eq}$ correlates with E_L
(Thevanayagam et al. 2003)

Working Hypothesis

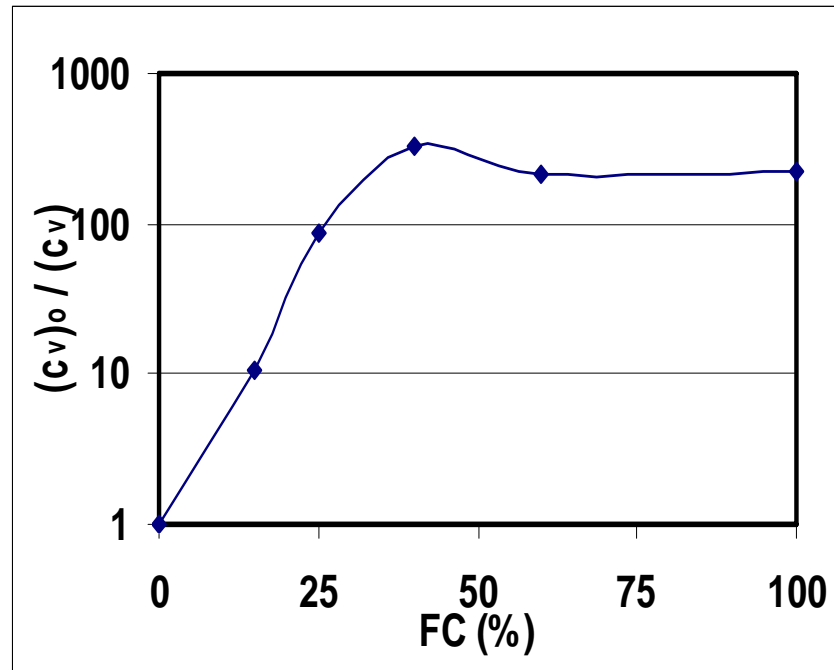
- Liquefaction resistance depends primarily on;
 - Inter-grain Contact Density
 - Contact density depends on e and silt content (FC)
- Permeability and compressibility depend on silt content, soil gradation, soil mineral
- Penetration Resistance depends primarily on;
 - Inter-grain Contact Density
 - C_v
 - Instrument Geometry
 - Penetration rate

Permeability (k)



(Thevanayagam and Martin, 2001)

Coefficient of Consolidation (c_v)



(Thevanayagam and Martin, 2001)

- C_v → Decreases up to FC_{th} , about 30-40% Silt content
 → Unaffected by Silt content $> FC_{th}$
 → Not much dependent on contact density

Findings

At the same contact density indices between sand and silt-mixes;

- Some difference in compressibility (m_v)
- Major difference in coefficient of consolidation (c_v) and permeability (k)



C_v depends on FC and k

(Thevanayagam and Martin, 2001)

Working Hypothesis

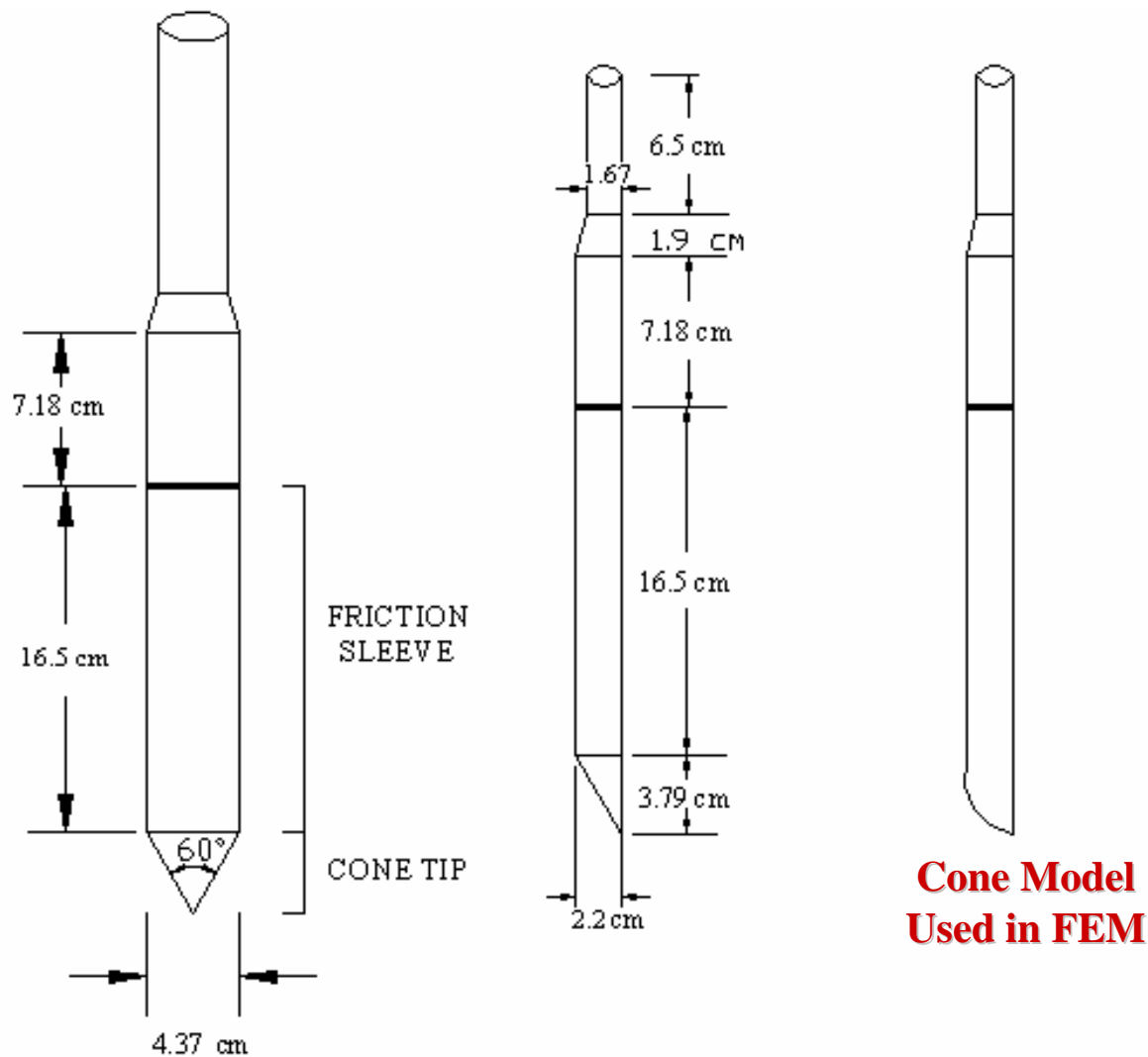
- Liquefaction resistance depends primarily on;
 - Inter-grain Contact Density
 - Contact density depends on e and silt content (FC)
- Permeability and compressibility depend on silt content, soil gradation, soil mineral
- Penetration Resistance depends primarily on;
 - Inter-grain Contact Density
 - C_v
 - Instrument Geometry
 - Penetration rate



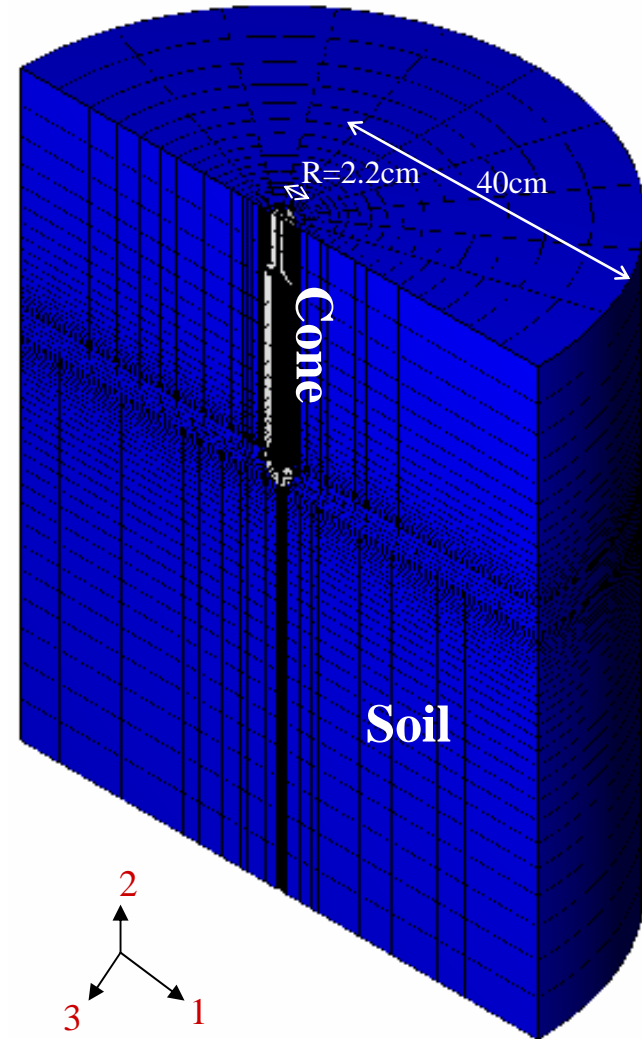
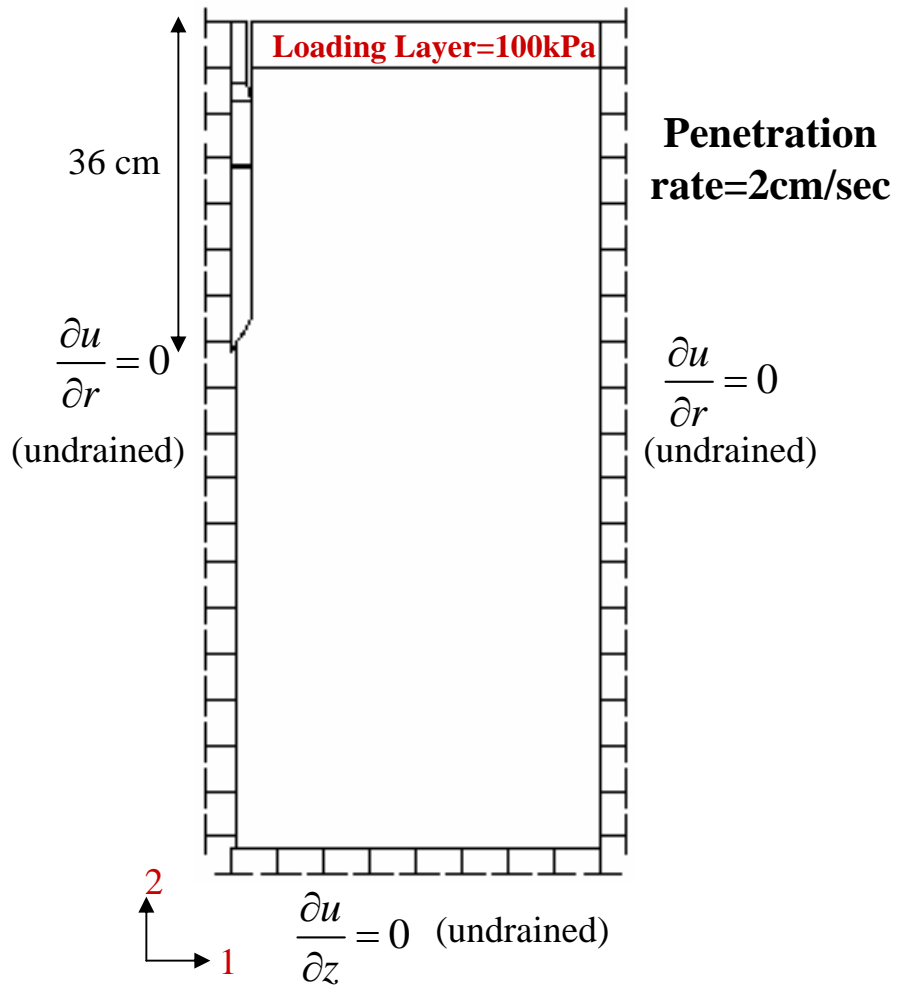
Effects of permeability and compressibility on

- Excess Pore Pressure response around the cone tip
- Cone penetration resistance

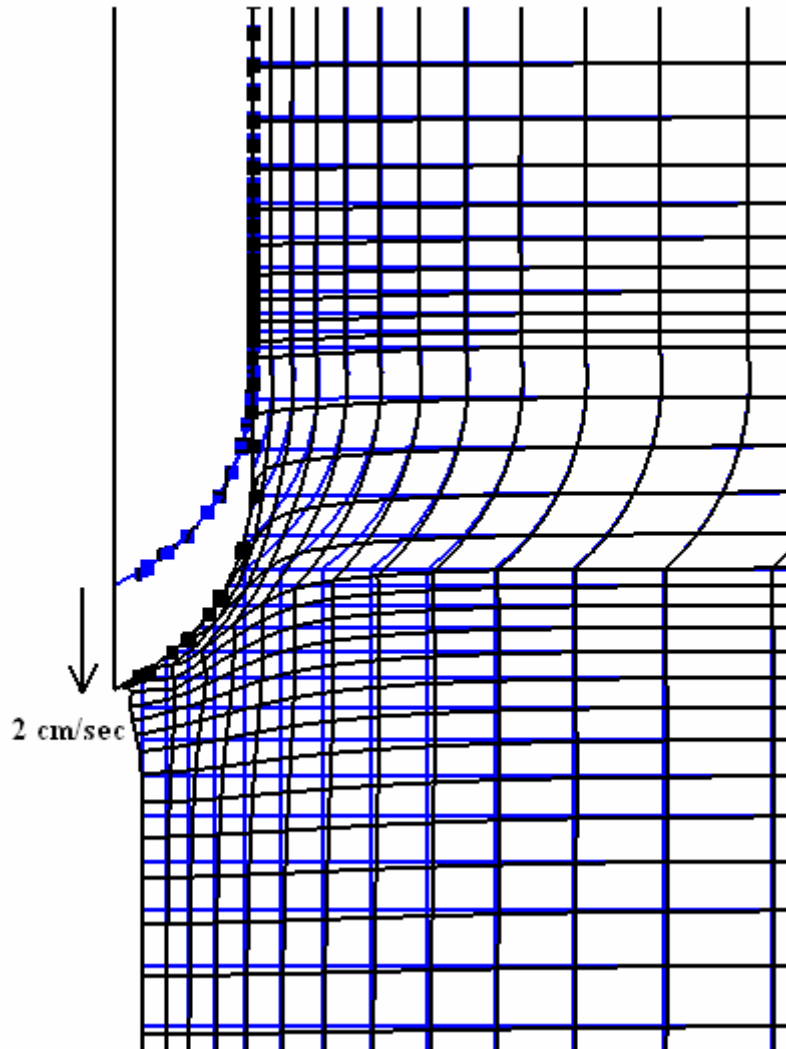
Cone Model Used in FEM



FEM Mesh

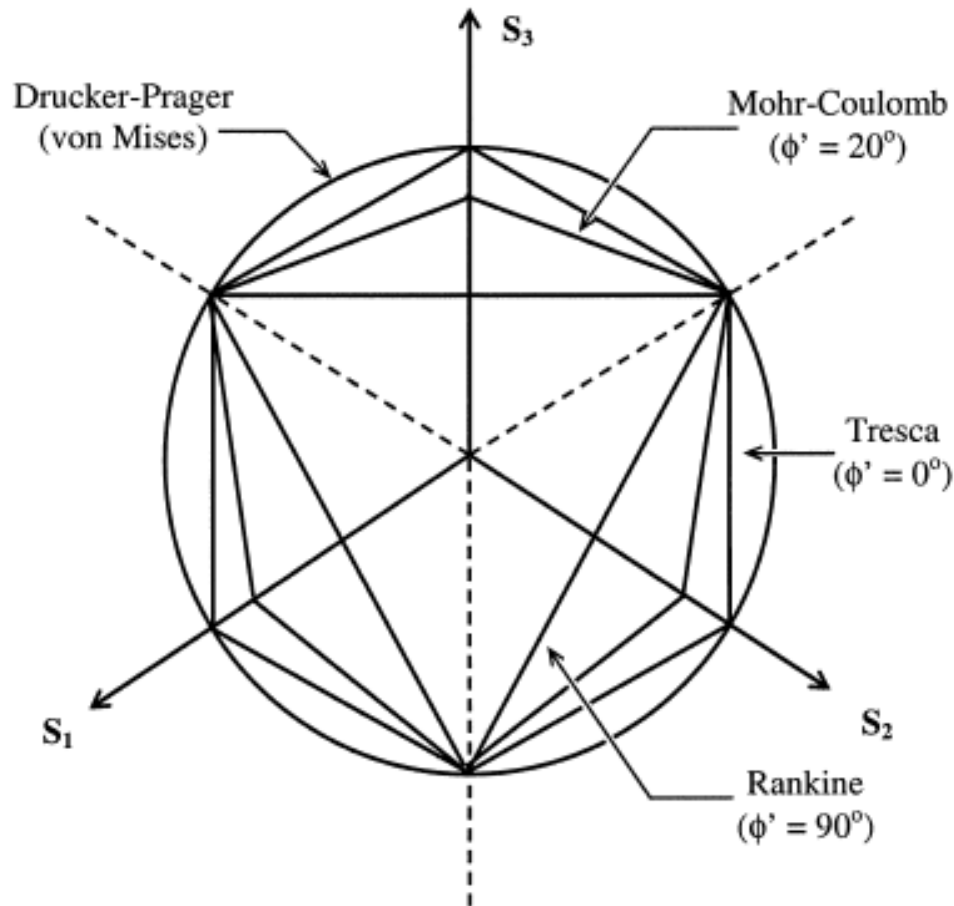


Finite Element Model



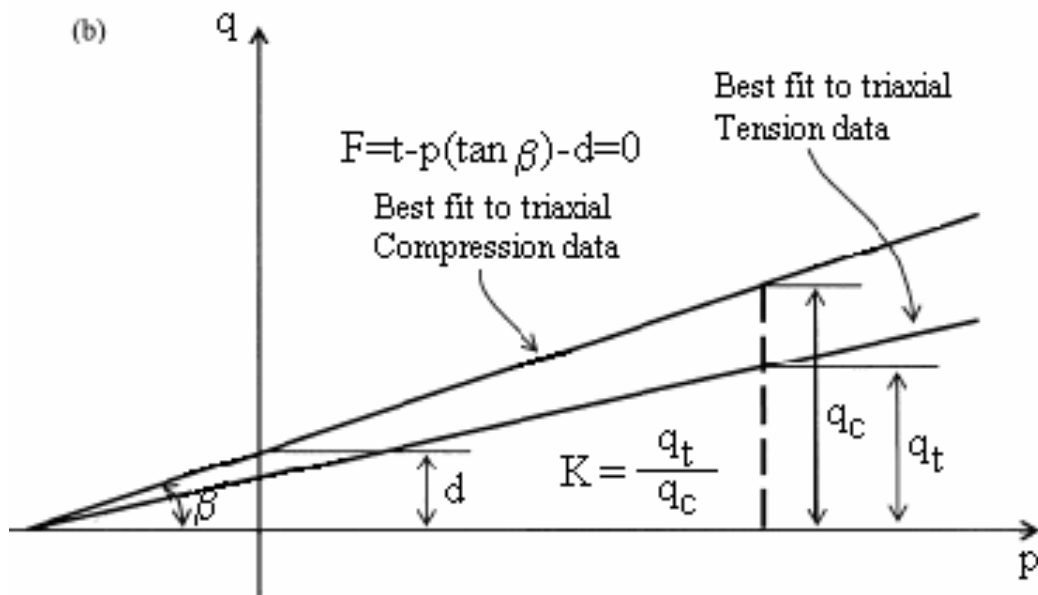
- Penetration rate 2 cm/s
- The area close to cone tip is under very large strain. Therefore to model the soil, a non-linear material constitutive model is used.

Soil Model (Drucker-Prager Model)



- Elastic Paramaters
- Yield Criterion
- Hardening Rule

Soil Model (Drucker-Prager Model)



Model parameters obtained from undrained monotonic triaxial tests.

$$F = t - (p \tan \beta) - d = 0$$

$$t = \frac{1}{2} q \left[1 + \frac{1}{K} - \left(1 - \frac{1}{K} \right) \left(\frac{r}{q} \right)^3 \right]$$

$$q = \tau_{oct} = \sqrt{\frac{2}{9} (I_1^2 + 3I_2)} = \sqrt{\frac{2}{3}} J_2$$

$$p = \sigma_{oct} = \frac{1}{3} I_1$$

Time Stepping and Accuracy

- Step 1: Equalizes geostatic loading
- Step 2: Small time increments for non-linear analysis

$$\Delta t \geq \frac{1}{6} \frac{(\Delta l)^2}{\theta c} \quad (\text{Vermeer and Verruijt 1981})$$

Δt =Time increment

Δl =Typical element dimension

θ =represents the type of approximation chosen for the behavior of the excess pore pressure

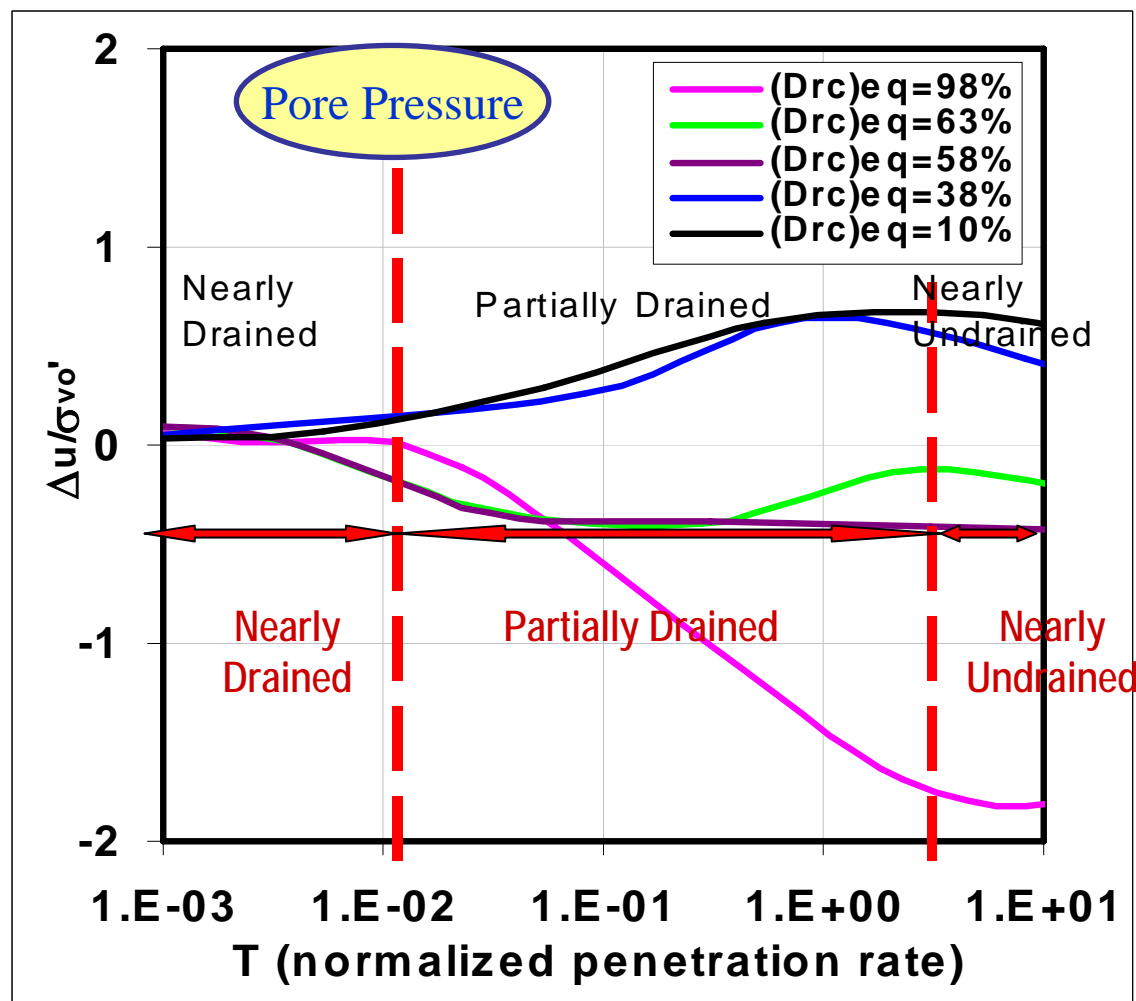
c =coefficient of consolidation

Normalized Penetration Rate (T) – Dependent Excess Pore Pressures and Cone Resistance

$$T = \frac{vd}{c_h}$$

- v = penetration rate (2cm/s : ASTM D3441)
- d = cone diameter (instrument geometry)
- c_h = coefficient of consolidation

$\Delta u/\sigma_{vo}$ vs normalized penetration rate



- Nearly 'drained' response at Low T values (**sands**)
- Partial drainage around the cone at intermediate T (**low silt content**)
- Nearly 'undrained' response at high T values (**high silt content**)

Preliminary Analysis

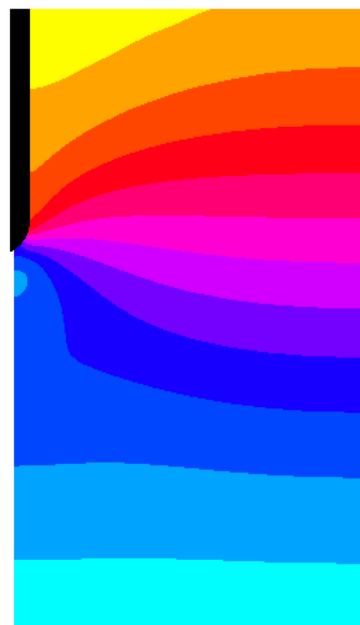
Effect of k and C_v on excess pore pressure contours around the cone tip

- $(D_{rc})_{eq} = 45\%$, $k = 10^{-3} \text{ m/s}$ \longrightarrow Dr=45%_k=10-31.wmv
- $(D_{rc})_{eq} = 45\%$, $k = 10^{-5} \text{ m/s}$ \longrightarrow Dr=45%_k=10-51.wmv
- $(D_{rc})_{eq} = 45\%$, $k = 10^{-7} \text{ m/s}$ \longrightarrow Dr=45%_k=10-71.wmv

Effect of "T" on Pore Water Pressure

Same material properties for all, but k was varied from 10^{-3} to 10^{-7} m/s

Pwp changed from negligible (drained) to significant (undrained)



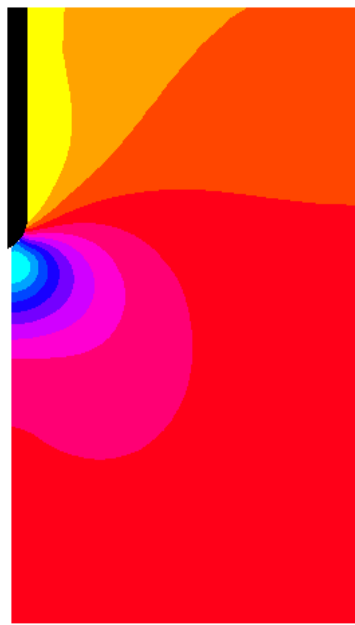
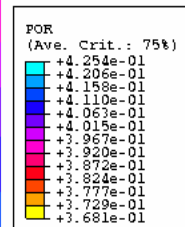
Primary Variable: Pore Water Pressure

Test Data: 7/12/1999

$(D_{rc})_{eq}=45\%$

$T=3 \times 10^{-4}$

Dilation Angle= 5°



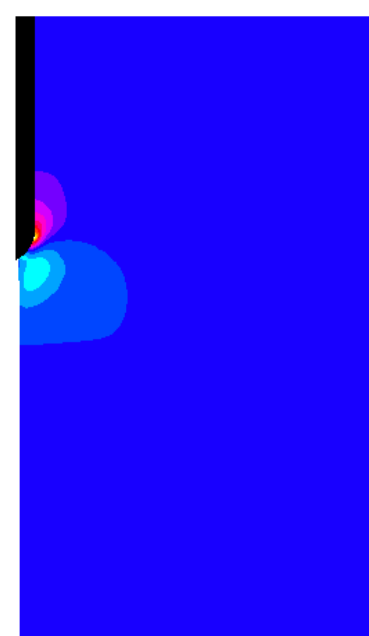
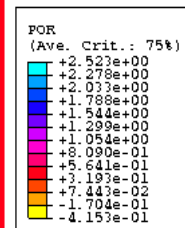
Primary Variable: Pore Water Pressure

Test Data: 7/12/1999

$(D_{rc})_{eq}=45\%$

$T=3 \times 10^{-2}$

Dilation Angle= 5°



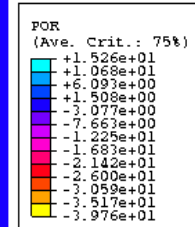
Primary Variable: Pore Water Pressure

Test Data: 7/12/1999

$(D_{rc})_{eq}=45\%$

$T=3$

Dilation Angle= 5°



$T=3 \times 10^{-4}$ ($k=10^{-3}$ m/s)

$T=3 \times 10^{-2}$, $k=10^{-5}$ m/s

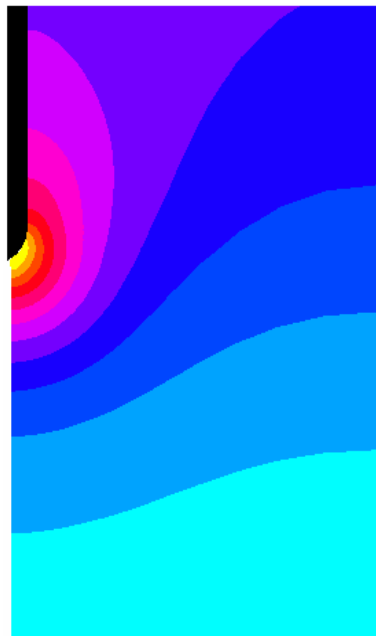
$T=3$, $k=10^{-7}$ m/s

$(D_{rc})_{eq}=45\%$

Effect of "T" on Pore Water Pressure

Same material properties for all, but k was varied from 10^{-3} to 10^{-7} m/s

Pwp changed from negligible (drained) to significant (undrained)



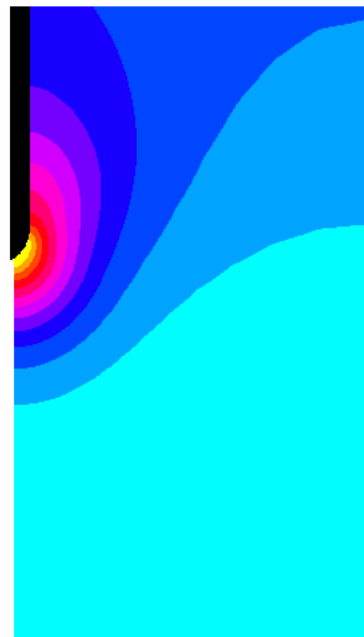
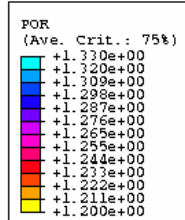
Primary Variable: Pore Water Pressure

Test Data: 3/12/1999

$(D_{rc})_{eq}=58\%$

$T=3 \times 10^{-4}$

Dilation Angle= 13°



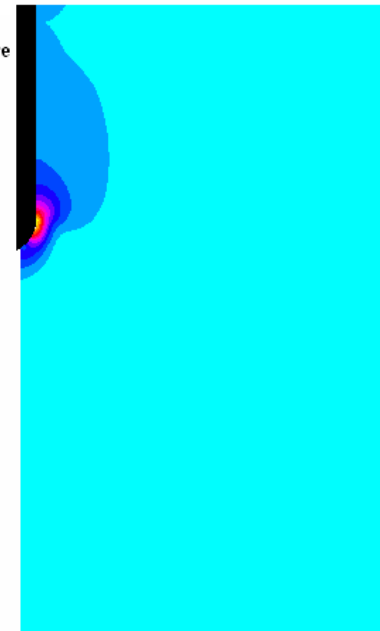
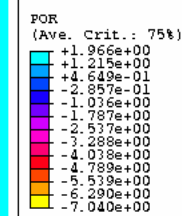
Primary Variable: Pore Water Pressure

Test Data: 3/12/1999

$(D_{rc})_{eq}=58\%$

$T=3 \times 10^{-2}$

Dilation Angle= 13°



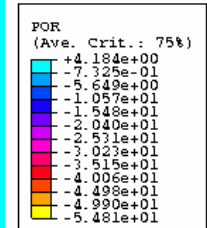
Primary Variable: Pore Water Pressure

Test Data: 3/12/1999

$(D_{rc})_{eq}=58\%$

$T=3$

Dilation Angle= 13°



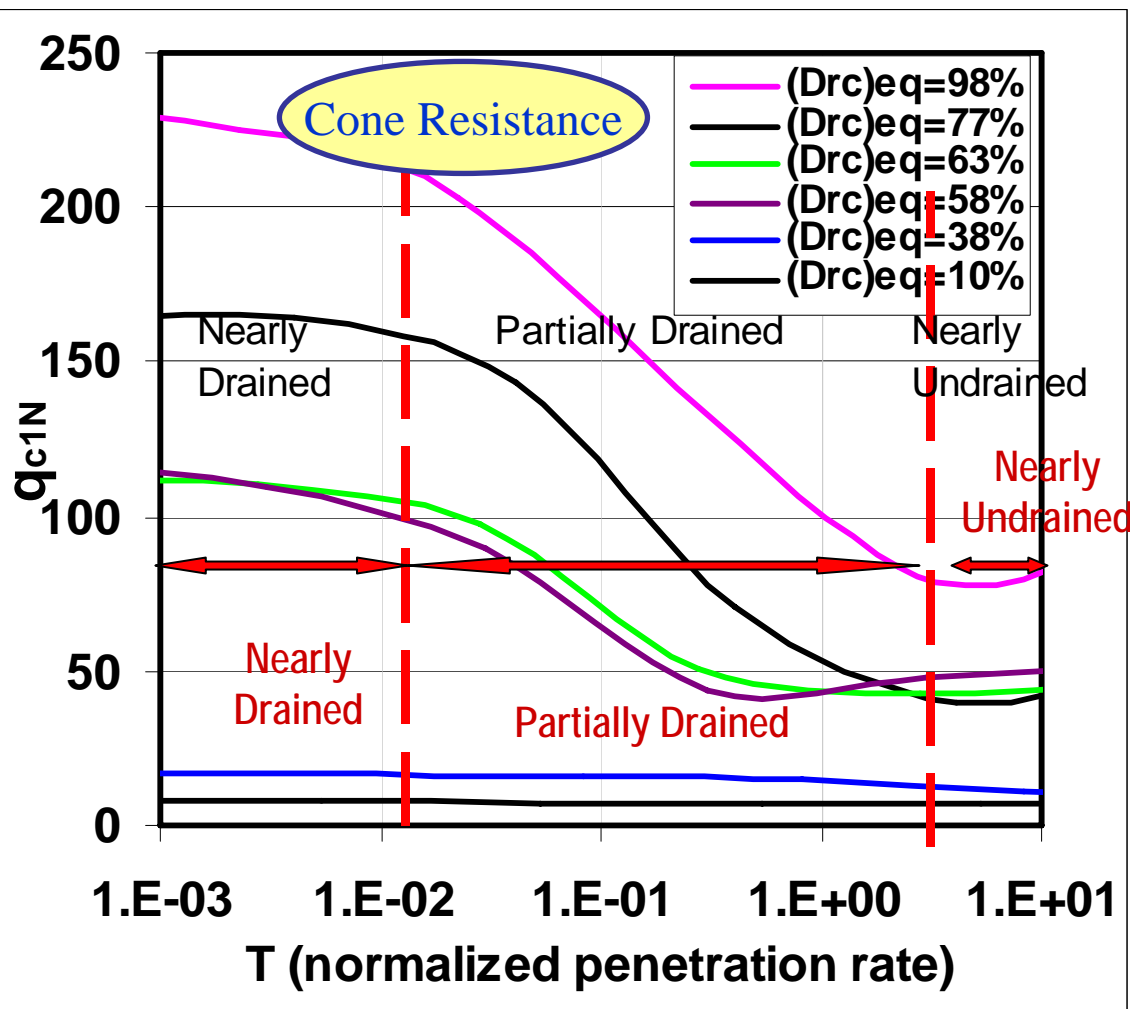
$T=3 \times 10^{-4}$ ($k=10^{-3}$ m/s)

$T=3 \times 10^{-2}$, $k=10^{-5}$ m/s

$T=3$, $k=10^{-7}$ m/s

$(D_{rc})_{eq}=58\%$

q_{c1N} vs normalized penetration rate



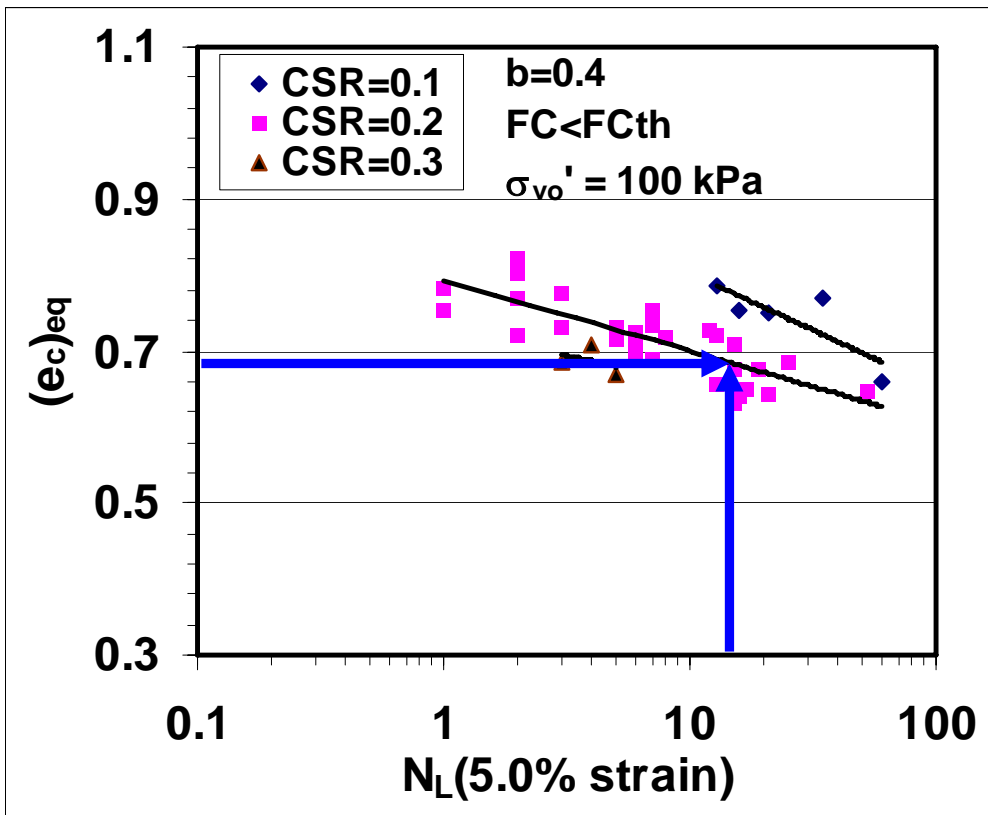
- Nearly 'drained' response at Low T values (**sands**)
- Partial drainage around the cone at intermediate T (**low silt content**)
- Nearly 'undrained' response at high T values (**high silt content**)



Effects of fines content on

- $(CRR)_{\text{field}}$ versus Cone Penetration Resistance
- E_L/σ_c' versus Cone Penetration Resistance

From Experimental Work



$(e_c)_{eq}$ & for 15cycles



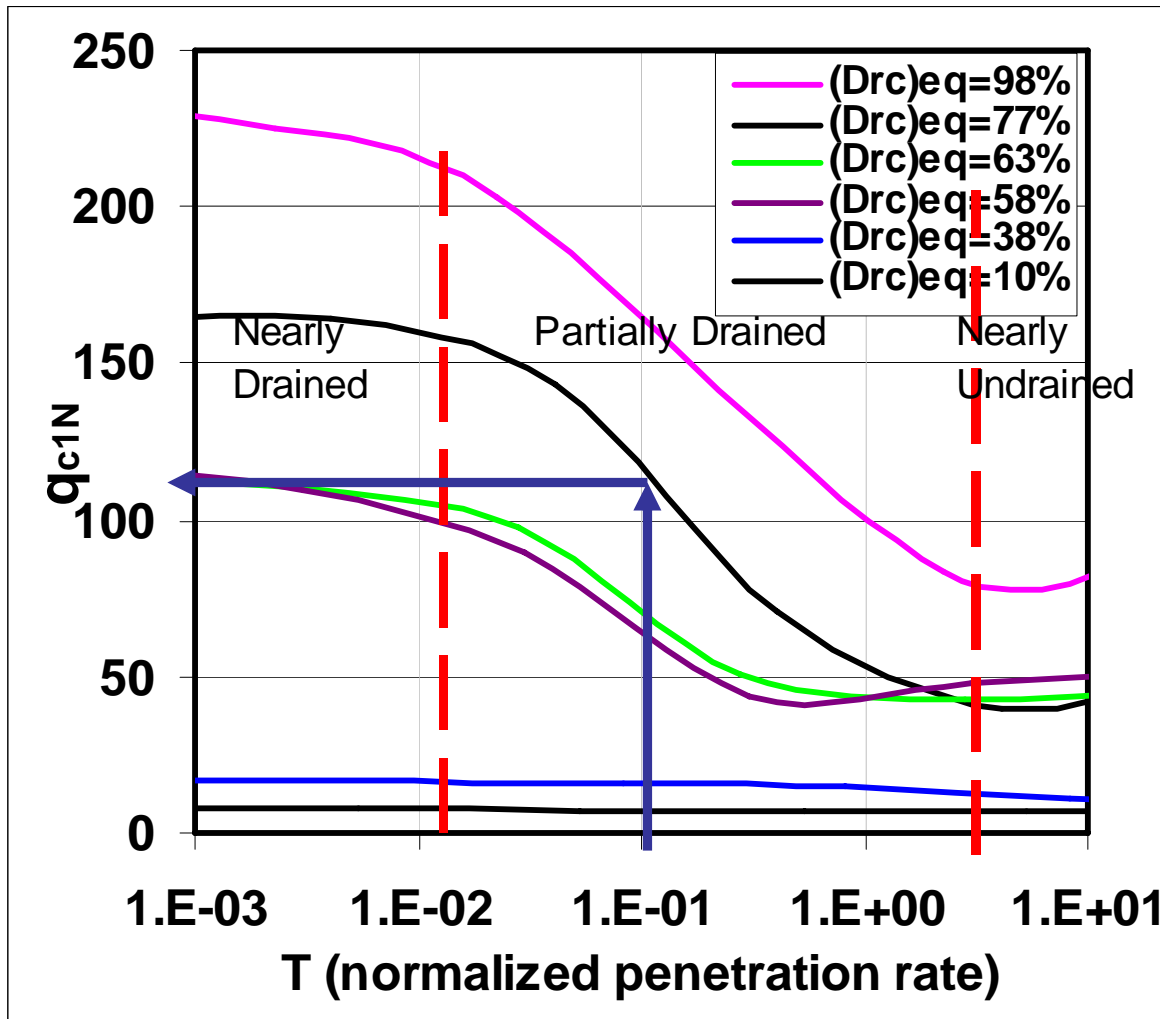
$(CRR)_{tx}$



$$(CRR)_{field} = 0.9 \frac{2(1 + 2K_o)}{3\sqrt{3}} (CRR)_{tx}$$

(Source : Castro (1975), Seed et al. (1978))

From Numerical Work

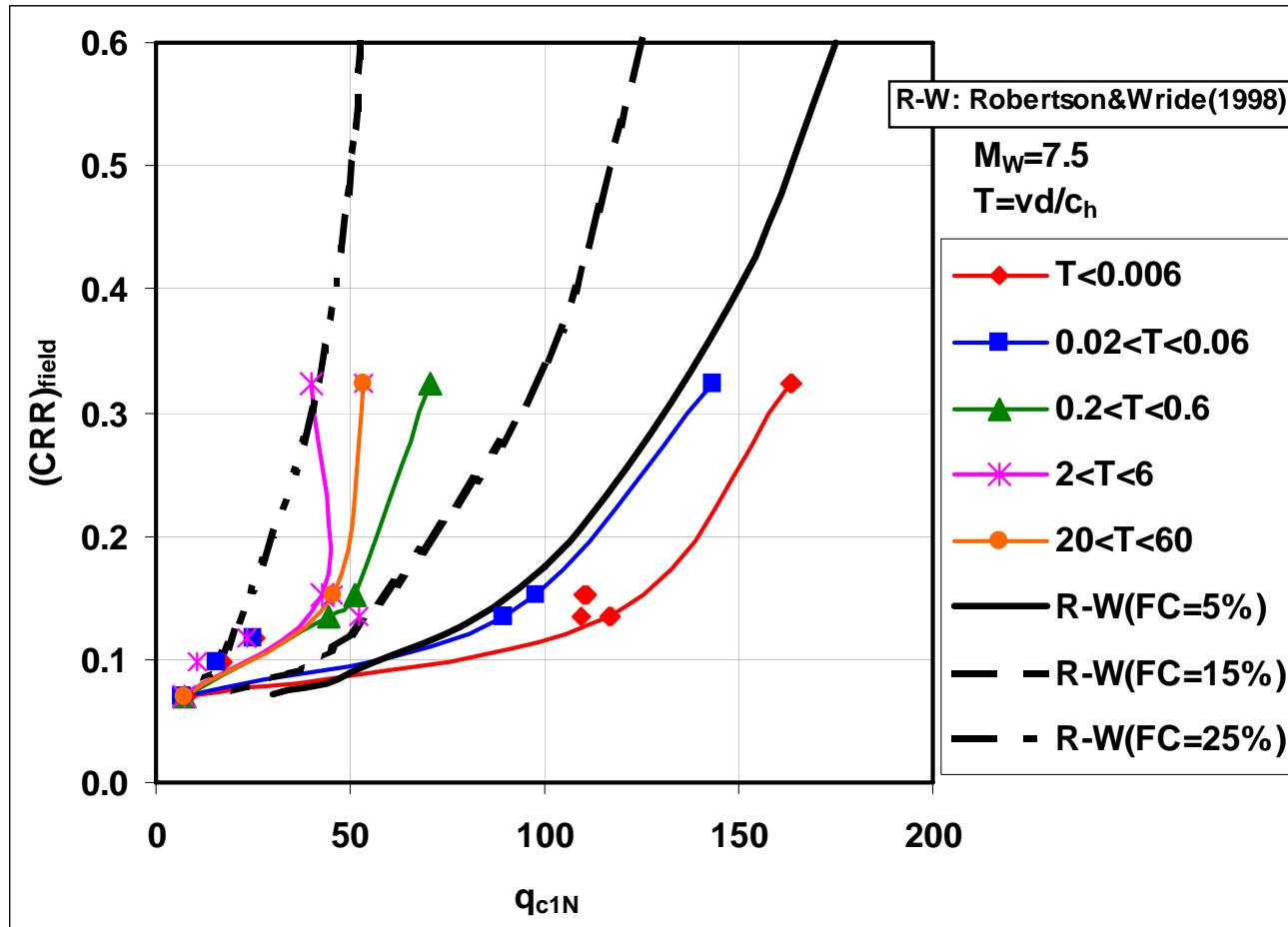


T & for $(D_{rc})_{eq}$

q_{c1N}

Proposed Liquefaction Screening

Based on CRR, q_{c1N} and T



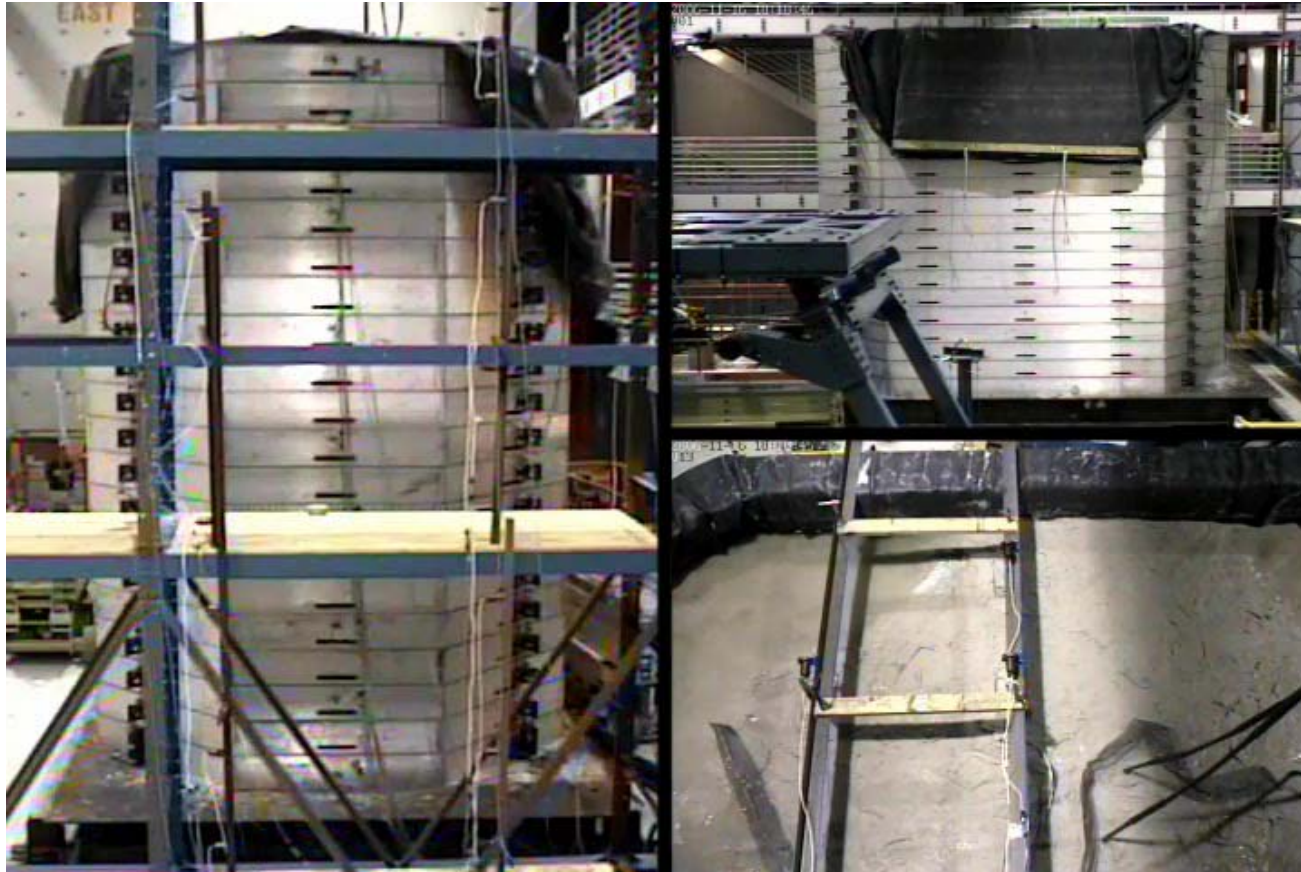
$$T = \frac{v_d}{c_h}$$

FC

Large Scale Liquefaction Test

- Test LG0

(For video, click <https://central.nees.org/?projid=122&loc=Public#>)

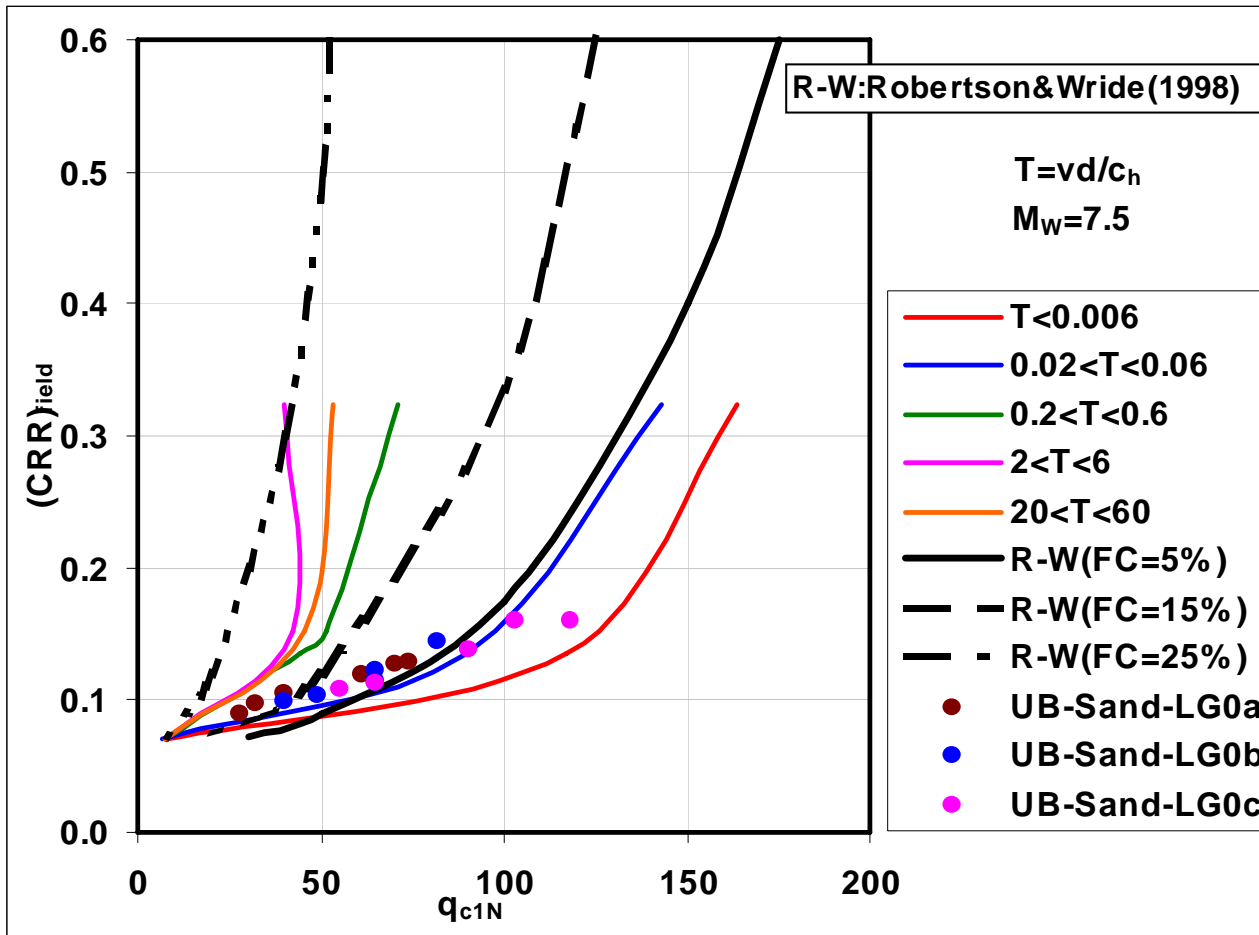


CPT tests before
shaking tests

Shake tests to
Liquefy soil

Compare CPT
resistance to
Liquefaction
Resistance

$(CRR)_{field} - q_{c1N} - T$ Relationship



FINDINGS

1. CRR depends on Intergrain Contact Density

- Contact density depends on e and silt content

2. Penetration Resistance depends primarily on

- Intergrain Contact Density
- Normalized Penetration Rate (T)
 - C_h
 - Instrument Geometry
 - Penetration rate

FINDINGS

3. CRR versus Penetration Resistance is Dependent on

- c_h , Cone geometry, size, and Penetration rate

4. CRR correlates with q_{c1N} & T

- $T = vd/c_h$
- c_h depends on silt content (and characteristics) and decreases up to a silt content of about 30-40%

5. CRR - q_{c1N} - T correlation is more rational than a mere silt-content dependent CRR- q_{c1N} - FC correlation, but requires further field validation and refinement



University at Buffalo

The State University of New York

THANK YOU
Questions..?