On the Weak Limestone Rock Slope Stability Analysis

G.L. Wilham¹

¹PT Signifikan Solusi Integrasi and Lecturer at Civil Engineering Dept., Postgraduate Program, National Institute of Science and Technology (ISTN), Jakarta, Indonesia ¹E-mail: wilham@signtegra.com and wilham.george@gmail.com

ABSTRACT: The natural rock slope of Weak Limestone has been studied, modelled analysis and reviewed. This paper describes the Rock Slope Stability Analysis for the construction of a Generating Station. Four scenarios were analysed i.e.: original proposal of 750; continuous slope of 60°; and double step slope of 60° and 60° with a bench; double Steep slope of 65° and 75° with a bench. Slope reinforcements (End Anchored and High Tensile Mesh) were recommended. The analysis is with Limit equilibrium method, LEM and Finite element method, FEM.

Keywords: Limestone, Rock Slope Stability, LEM, FEM.

1. INTRODUCTION

This paper describes the Slope Stability Analysis for the construction of a Generating Station. This paper aims to analyse the rock slope stability: A steep slope early proposed 750, and then propose the following;

- a. Steep slope of 60°
- b. Double Steep slope of 60° and 60° with a bench
- c. Double Steep slope of 65° and 75° with a bench
- **d.**Recommendation of slope reinforcement (End Anchored and High Tensile Mesh) if needed.

The main analysis conducted is aimed at finding the Factor of Safety (FS), through the Limit Equilibrium method using Rocscience's slope stability Analysis Software Slide 3D and with Finite Element Method (Griffiths 2015), and a Microsoft Excel Software.

2. CASE STUDY

2.1 Location

The drilling hole point at the nearest future Slope is at BHX depicted in Figure 1. Figure 2 showed the Borelog BH-X

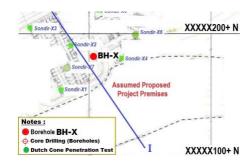


Figure 1 Assumed Geotechnical Investigation Area

2.2 Seismic Condition

The Earthquake Strong Ground Motion properties was calculated using the expected peak ground acceleration for Probability Exceeding 2% in 50 Years, according to the Indonesian Earthquake Hazard Map (Ministry of Public Work 2017) for the maximum credible earthquake at our study site in Eastern Indonesia. The resulting PGA from the Earthquake Hazard Map was 0.5 g. A moment magnitude of Mw = 8.0 was used based on W.G. Housner's chart (1971). Figure 4 and Figure 5 depict the Indonesian Earthquake Hazard Map and Housner's Recommendation Table for Strong Ground Motion.

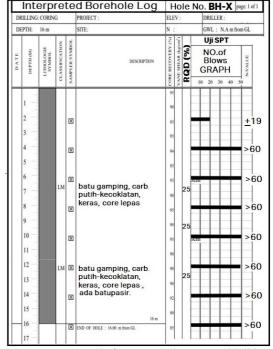


Figure 2 An example only for a Borehole BH-X, with lithology of LIMESTONE that shown the Low Values of RQD (ranging from 0 to 25%)

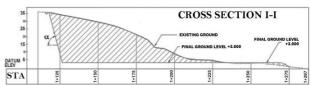


Figure 3 Site (Previously) Planned Cross Section Profile

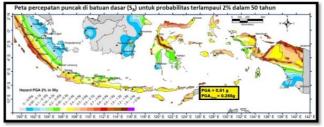


Figure 4: The Peak Ground Acceleration Map in Bedrock (Sb) for Probability Exceeding 2% in 50 Years (For our site, The PGA = 0.51 g, and the Acceleration Multiplier is 0.5).

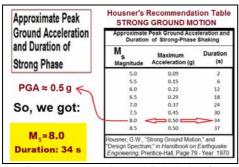


Figure 5: GW Housner's Table and Calculation for Mw and Earthquake Duration - Maximum Peak Ground Acceleration at Bedrock

2.3 Laboratory Test Results

Based on the Rock Laboratory and Point Load tests, we found out that the Limestone in the area is weak Limestone, with UCS = 1800 kPa, Young's Modulus, E = 250000 kPa and Poisson's Ratio, v = 0.23.

Through additional analysis of Rockmass Properties we found out that the Rock mass is FAIR (Q or NGI Classification), with GSI = 41. (See Appendix C).

2.4 Ground (Soil) Resistivity Test Results

Based on the Soil Resistivity test, we found out that the Limestone in the area is a weak Limestone, Figure 6 showed the summary of it.

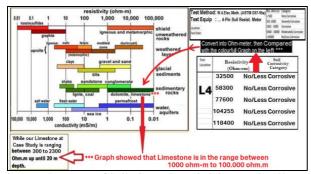


Figure 6. Summary of Soil (Ground) Resistivity Results (Showed the type of Limestone that is in the range of weak rock, which is anomaly from the common Limestone found elsewhere.)

3. METHODS OF ANALYSIS

3.1 Limit Equilibrium Method (LEM)

LEM is a method that uses the principle of force equilibrium. This method of analysis first assumes the field of sliding that can occur, the field of assumption that is assumed to be circular and non-circular (Figure 7)

LEM is the most popular approach in slope stability analysis. This method is well known to be a statically indeterminate problem, and assumptions on the interslice shear forces are required to render the problem statically determinate. Based on the assumptions of the internal forces and force and/or moment equilibrium, there are more than 10 methods developed for slope stability analysis. The famous methods include those by Janbu (1957, 1973), Spencer (1967) and Morgenstern and Price (1965).



Figure 7. Failure Line: Circular & Non-Circular+ +The calculation is done by dividing layers of rock / soil that are in the field of landslides into slices.

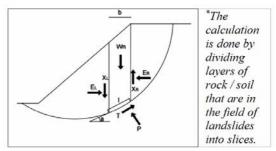


Figure 8. Forces that work in the Slices*

All these methods consider the moment and force equilibrium in each slice. If the moment and force equilibrium is satisfied in each slice, the overall moment and force equilibrium will be satisfied automatically. The basic concept in these methods is the same; the difference lies in the assumption of the interslice forces. If both moment and force equilibrium are satisfied, the assumption on interslice forces should have only small effect on the factor of safety obtained.

In the Morgenstern and Price method, an assumption is made regarding the relationship between interslice shear and normal forces. After obtaining the computer output based on this assumption, all the computed quantities, including the inter-slices forces, must be examined to determine whether they seem reasonable. If not, a new assumption must be made.

All these methods can be applied to both circular and noncircular failure surfaces.

3.2 The failure criterion for intact rock (Limestone)

In rock mechanics practice the use of Hoek-Brown failure criteria is common. The Hoek-Brown properties (GSI, mi and s) can be converted into Mohr-Coulomb intact rock properties (ϕ and c).

a. Mohr Coulomb Failure Criterion

The failure criterion for intact rock used is the Mohr-Coulomb criterion as follows, $\tau_i = \sigma_{ni} \tan \phi_o + c_o$; where σ_{ni} is the normal stress on the failure plane and ϕ_o and C_o are material constants for intact rock (Appendix C).

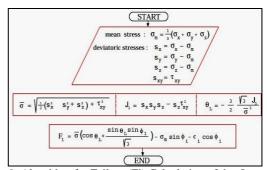


Figure 9. Algorithm for Failure (Fi) Calculation of the Intact Rock (Limestone).

b. Generalized Hoek-Brown Failure Criterion (constitutive Model) For a constitutive Model of the Generalized Hoek-Brown (Hoek 1995; Eberhardt 2012), the equation is as follows:

$$\sigma_1 - \sigma_3 - \sigma_{ci} \left(m_b \frac{\sigma_3}{\sigma_{ci}} + s \right)^a = 0 \tag{1}$$

Where σ_1 dan σ_3 are major and minor principal stress, σ_{ci} is unconfined compressive strength (UCS) or the maximum axial compressive stress that a right-cylindrical sample of material can withstand under unconfined conditions — the confining stress is zero, and

$$m_b = m_i \exp\left(\frac{GSI - 100}{28 - 14D}\right) \tag{2}$$

$$s = \exp\left(\frac{GSI - 100}{9 - 3D}\right) \tag{3}$$

$$a = \frac{1}{2} + \frac{1}{6} \left[\exp\left(\frac{GSI}{15}\right) - \exp\left(\frac{-20}{3}\right) \right]$$
 (4)

mi is a material constant for the intact rock, GSI (the Geological Strength Index) relates the failure criterion to geological observations in the field, and D is a "disturbance factor" which depends upon theo of disturbance to which the rock mass has been subjected by blast damage and/or stress relaxation. It varies from 0 for undisturbed in situ rock masses to 1 for very disturbed rock masses.

3.3 The Finite Element Method (FEM)

The FEM is a numerical method for solving problems of engineering and mathematical physics. Typical problem areas of interest in engineering and mathematical physics that are solvable by use of the finite element method include structural analysis, geotechnical engineering (inc'l Slope Stability, Tunneling etc.), heat transfer, fluid flow, mass transport, and electromagnetic potential.

The majority of slope stability analyses performed in practice still use traditional limit equilibrium approaches involving methods of slices that have remained essentially unchanged for decades. Then, in 1967, Whitman & Bailey (1967) set criteria for the then emerging methods to become readily accessible to all engineers (Louhenapessy 1995). The FEM represents a powerful alternative approach for slope stability analysis which is accurate, versatile and requires fewer a priori assumptions, especially, regarding the failure mechanism. The author will use Griffiths' FEM Software, name: SLOPE64 (Griffiths 2004, Griffiths & Lane 1999) to check the Limestone Rock Slope Stability.

4. ASSUMPTIONS

The calculation of the factor of safety of the given slope was conducted, which is done depending on the rock material properties (based on Mohr-Coulomb and/or Hoek-Brown Constitutive Model), the slope geometry, static (live) load (10 kPa on top of the slope), Seismic Load (0.255 g) and if necessary the slope reinforcement.

The two loadings that were used were Non-Earthquake (NE) loading, and Earthquake (E) loading. Earthquake loading was provided from Figure 4, The Peak Ground Acceleration Map in Bedrock (Sb) for Probability Exceeding 2% in 50 Years (Peta Percepatan Puncak di Batuan Dasar (Sb) Untuk Probabilitas Terlampaui 2% Dalam 50 Tahun) by The Public Work Department Republic of Indonesia.

Recommended values of safety factors for rock slopes use, SF > 1.5 reference RSNI "Persyaratan Perancangan Geoteknik BSNI 2017. Recommendation of earthquake values of safety factors using, SF > 1.0 Hynes-Griffin and Franklin (1984). (Figure 10).

Condition of rock slope	Recommended safety factor values	(1)	(2) Reference Acceleration,	(5) Minimun Factor of
		Reference	$a_{\rm ref}$	Safety
Permanent condition	1.5	Seed (1979)	$0.75g\left(M\approx6\frac{1}{2}\right)$	1.15
	7.0	Seed (1979)	$0.75g\left(M \approx 8\frac{1}{4}\right)$	1.15
Temporary condition	1.3	Hynes-Griffin and	$PGA_{mod}(M \le 8.3)$	1.0
eference : RSNI3 Persyarata	Hynes-Griffin and Franklin (1984)	$PGA_{rock}(M \le 8.3)$	1.0	
BSNI - Page134	32.5	Bray et al. (1998)	PGA _{rock}	1.0

Figure 10: Safety Requirement: Above Left Column, shows that earthquake loading Factor of Safety requirement is 1.5 (Permanent Condition), whilst other common practice, such as Hynes-Griffin

and Franklin (1984) showed that the Safety Factor for earthquake loading should be no less than 1.0. See (Right Column Above).

5. RECOMMENDATION AND CONSLUSION

It is recommended that using The Slope Angle of 60°s without Shotcrete (but instead will use High Tensile Mesh) and using endanchor of 5 m x 5 m, with 15 m long and 100 kN tensile capacity.

Table 1 and Table 2 below details the results of the slope stability analysis (72 Run) along with the loadings (static and seismic) and some of the reinforcements that were provided.

Table 3 showed that from the Matrix of Percentage for Factor of Safety compared with Required Factor of Safety, the best option for design is using the double slope of 600 dip angle. While a Table in Appendix D, is the FEM Summary Results.

The above recommendation is still a bit higher than the one recommended by Rodrigues (Appendix B), where in his Table 6.5, Rodrigues et.al. recommend that (for broken Limestone) a double slope with first slope angle is 53° and a higher level slope is 450 angle. The chosen of broken Limestone is due to the Rock Mechanics Lab. Results and the broken/low values of RQD (Figure 2).

It is recommended to check the tension crack and make sure if there are joint rock appears in the weak limestone the dip angle of the joint rock should be lower than 20° (Appendix E).

Table 1 Summary of Without Shotcrete (Instead, now with: High-Tensile steel wire and Erosion Control)

				z		r p p	Safet	y Factor	FIGURE A	
Slope Geometry	Top Stope Angle (Degree)	Bottom Slope Angle(Degree)	Material Model / Method	Reinforcement (End Anchor) YIN	Groundwater	Load (Static is 10 kPa), and Eartquake 50% of 0.51 PGA	Morgensten-Price	MEAN from two (Least) Limit Equilibrium Method	Indonesian Code for Geotech Requirement (RSNI 2017 & Hynes- Griffin 1894, See Appendix B)	
63	75	64	Mohr-Coulomb	NO	YES	Static	2.029	2.032	1.500 A1	
Double	75	64	Mohr-Coulomb	NO	YES	Earthquake	1432	1.411	1.000	
Sic	75	64	Hoek Brown-D0	NO	YES	Static	1388	1.356	1.500 A9	
20	75	64	Hoek Brown-D0	NO	YES	Earthquake	0.999	0.942	1.000	
Slope	75	64	Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	2.042	2.043	1.500 A7	
Double Slope	75 64		Mohr-Coulomb	YES (as above)	YES	Earthquake	1.435	1.414	1.000	
	75	64	Hoek Brown-D0	YES (as above)	YES	Static	1.404	1.374	1.500 A8	
ā	75 64		Hoek Brown-D0	YES (as above)	YES	Earthquake	1.018	0.959	1.000	
Double Slope	60	60	Mohr-Coulomb	NO	YES	Static	2.026	2.043	1.500 A6	
	60	60	Mohr-Coulomb	NO	YES	Earthquake	1.433	1.414	1.000	
Sic	60	60	Hoek Brown-D0	NO	YES	Static	1.400	1.365	1.500 A5	
-	60	60	Hoek Brown-D0	NO	YES	Earthquake	1.011	0.948	1.000	
	75		Mohr-Coulomb	NO	YES	Static	1.921	1.699	1.500 A4	
Single	75		Mohr-Coulomb	NO.	YES	Earthquake	1.422	1.219	1.000	
Sign	75		Hoek Brown-D0	NO	YES	Static	0.991	0.976	1.500 A1	
	75		Hoek Brown-D0	NO	YES	Earthquake	0.702	0.673	1.000	
e	60		Mohr-Coulomb	NO	YES	Static	1897	1.898	1.500 A2	
dol	60		Mohr-Coulomb	NO	YES	Earthquake	1397	1.376	1.000	
e S	6	0	Hoek Brown-D0	NO.	YES	Static	1286	1.253	1500 A3	
Single Slope	60		Hoek Brown-D0	NO.	YES	Earthquake	0.927	0.880	1.000	
Single Slope	6	0	Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	1,925	1.924	1500 A1	
9	6	0	Mohr-Coulomb	YES (as above)	YES	Earthquake	1.414	1.391	1.000	
ing	6	0	Hoek Brown-D0	YES (as above)	YES	Static	1.317	1.287	1.500 A1	
S	6	0	Hoek Brown-D0	YES (as above)	YES	Earthquake	0.953	0.904	1.000	

Table 2 Summary (with Shotcrete: Not Recommended, due to sShotcrete is Prone to Groundwater and Can Crack)

				Safety Fac		y Factor	A		
Slope Geometry	Slope Geometry Top Slope Angle (Degree) Model Angle(Degree) Angle(Degree)		Material Model / Method	Reinforcement (End Anchor) Yi	Groundwater	Load (Static is 10 kPa), and Eartquake 50% of 0.51 PGA	Morgensten-Price	MEAN from two (Least) Limit Equilibrium Method	Indonesian Code for Geotech Requiement (RSM 2017 & Hynes- Griffin 1984, See Appendix B)
de	64	75	Mohr-Coulomb	NO	YES	Static	2.015	2.060	1.500
Double	64	75	Mohr-Coulomb	NO	YES	Earthquake	1444	1.430	1.000
S	64	75	Hoek Brown-D0	NO	YES	Static	1.104	1.101	1.500
- 4	64	75	Hoek Brown-D0	NO	YES	Earthquake	0.741	0.716	1.000
Double	64	75	Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	2.028	2.074	1.500
Slope	64	75	Mohr-Coulomb	YES (as above)	YES	Earthquake	1.454	1.437	1.000
0 0	64	75	Hoek Brown-D0	YES (as above)	YES	Static	1.204	1.203	1.500
	64	75	Hoek Brown-D0	YES (as above)	YES	Earthquake	0.837	0.818	1.000
0	60	60	Mohr-Coulomb	NO	YES	Static	2.012	2.057	1.500
Double	60	60	Mohr-Coulomb	NO	YES	Earthquake	1.435	1.418	1.000
Do IS	60	60	Hoek Brown-D0	NO	YES	Static	1248	1.239	1.500
	60	60	Hoek Brown-D0	NO	YES	Earthquake	0.853	0.829	1.000
Double	60	60	Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	2.026	2.068	1.500
do do	60	60	Mohr-Coulomb	YES (as above)	YES	Earthquake	1.438	1.420	1.000
S D	60	60	Hoek Brown-D0	YES (as above)	YES	Static	1.321	1.319	1.500
	60	60	Hoek Brown-D0	YES (as above)	YES	Earthquake	0.930	0.907	1.000
Single Slope		5	Mohr-Coulomb Mohr-Coulomb	NO NO	YES YES	Static Earthquake	1823	1.748	1500 1,000
25.00	75 75		Hoek Brown-D0	NO NO	YES	Static	0.863	0.861	1500
119864	75		Hoek Brown-D0	NO NO	YES	Earthquake	0.564	0.529	1.000
Single Slope	75		Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	2.021	1.860	1.500
Sing		5	Mohr-Coulomb	YES (as above)	YES	Earthquake	1.206	1.208	1.000
0,0,	75 75		Hoek Brown-D0	YES (as above)	YES	Static	0.889	0.898	1.500
	7	5	Hoek Brown-D0	YES (as above)	YES	Earthquake	0.609	0.596	1.000
Single Slope	60		Mohr-Coulomb	NO	YES	Static	1.831	1.866	1.500
12.0	60		Mohr-Coulomb	NO	YES	Earthquake	1347	1.334	1.000
0, 0,	60		Hoek Brown-D0	NO	YES	Static	1.066	1.059	1.500
	- 6	10	Hoek Brown-D0	NO	TES	Earthquake	0.740	0.710	1.000
Single	ं	0	Mohr-Coulomb	YES 5x5, 100 kN, 15m	YES	Static	1.835	1.882	1.500
Single		0	Mohr-Coulomb	YES (as above)	YES	Earthquake	1349	1.341	1.000
0,0,		0	Hoek Brown-D0	YES (as above)	YES	Static	1.113	1.109	1.500
	- 6	0	Hoek Brown-D0	YES (as above)	YES	Earthquake	0.781	0.755	1.000

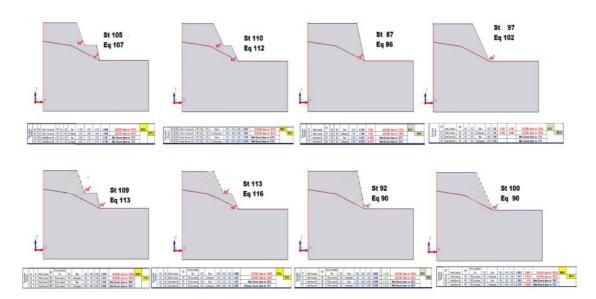
Notes: = Limit Equlibrium Method, FEM = Finite Element Method.

Table 3 Matrix of Percentage for FS compared with Required FS PS: The tables bellow each Slope Profile is taken from the Table 1

Matrix of Percentage for Factor of Safety compared with Required Factor of Safety

Percentage of Safety Factor compared to the Required Safety (St = For Mean Values of Mohr Coulomb and Hoek Brown Static Slope Stability Analysis)

(Eq = For Mean Values of Mohr Coulomb and Hoek Brown with Earthquake Slope Stability Analysis)



6. REFERENCES

- Eberhardt, E. (2012) "The Hoek-Brown Failure Criterion", Rock Mech Rock Eng Vol. 45:981–988.
- Griffiths, D.V.& Lane, P.A. (1999) "Slope stability analysis by finite elements", Geotechnique Vol. 49, No. 3, pp. 387-403.
- Griffiths, D.V. (2015) SLOPE STABILITY ANALYSIS BY FINITE ELEMENTS A guide to the use of Program Slope64, Geomechanics Research Center Colorado School of Mines, September 2015
- Haynes-Griffin, M.E. and Franklin, A.G. (1984) "Rationalizing The Seismic Coefficient Method", Dept. of The Army, US Army Corps of Engineers
- Hoek, E., Kaiser, P.K. and Bawden, W.F. (1995) "Support of Underground Excavations in Hard Rock", AA Balkema, Rotterdam.
- Louhenapessy, W. G. The Computer Algorithm Failure Index for joint rock mass in Tunnelling Design, Slope Stability and Well bore Stability Jurnal Teknik Sipil: No.2, Tahun ke IX, Jul. 2003, hal.: 277-293, Tarumanagara University, Jakarta, Indonesia.
- Louhenapessy, W. G. & Pande, G.N. (2000) Newmo3962_2000: User's Instruction Manual, Internal Rep.No.CR/1022/00. Dept. of Civil Eng., Univ. of Wales Swansea, 2000.
- Louhenapessy, W. G. (1995) "Undrained Analysis of Rock Structures", MSc Thesis, University of Wales, Swansea.
- RocNews (Spring 2017) "Slide3 Introducing 3D Limit Equilibrium Slope Stability Analysis , Rocscience, Toronto, Canada"
- Rodriquez, A.R., Del Castillo, H. and Sowers, G. (1988) "Soil Mechanics in Highway Engineering", 2nd Edition, Trans Tech Publication.
- Rockscience https://www.rocscience.com/software/slide3 RSNI (2017) "Persyaratan Perancangan Geoteknik BSNI 2017

APPENDIX A - Portion of LEM

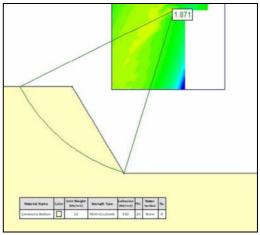
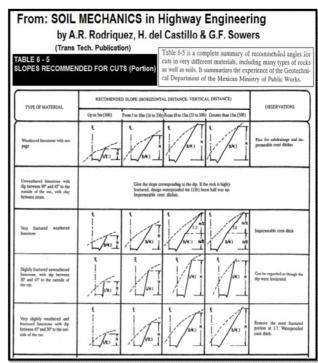


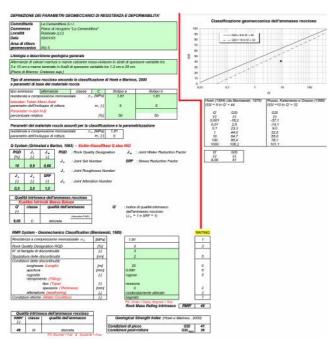
Figure A.1 Portion of LEM Results (by Slide Software)

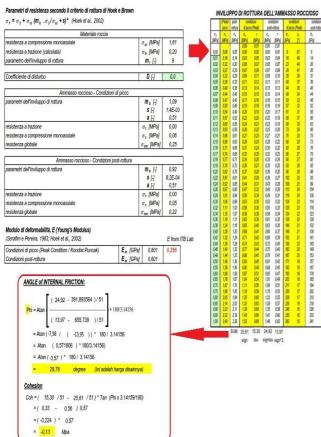
APPENDIX B - Slopes Recommended for Cuts



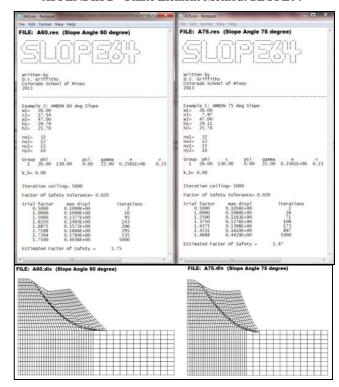
Rodrigues et.al. recommend that (for broken Limestone) a double slope with first slope angle is 53° and a higher level slope is 45° angle.

APPENDIX C - Rock Classification with Mohr Coulomb and Hoek-Brown Intact Rock Properties





APPENDIX D -Finite Element Method: SLOPE64





APPENDIX E – Tension Crack Analysis

Top Stope Angle (Degree)	Bottom Slope Angle(Degree)	Material Model / Method	With Shotrete (YRN)	Reinforcement (End Anchor) YW	Groundwater	Load (Static is 10 kPa), and Eartquake 50% of 0.51PGA	SE Jenston Crack Analysis	SF Mean Barthquake (MC+HB)	General Comment	Indonesian Code for George National Page 1847 Street Soffin 1884 See Appendix B.
60		Tension Crack (Excel)	NO	NO	YES	Static				
		20 degree joint			(Full)	Static	1994	133%	Good	1500
		20 degree joint			(Half)	Static	2.778	185%	Good	1500
		Tension Crack (Excel) 30 degree joint	NO	NO	YES (Full)	Static Static	1248	83%	Not Good	1500
		30 degree joint			(Half)	Static	1.697	113%	Good	1500
		Tension Crack (Excel) 40 degree joint	NO	NO	YES (Full)	Static Static	0.907	60%	Not Good	1500
		40 degree joint			(Half)	Static	1,287	86%	Not Good	1500
75		5 Tension Crack (Excel) 20 degree joint		NO	YES (Full)	Static Static	2.050	137%	Good	1500
		20 degree joint			(Half)	Static	2.968	198%	Good	1500
		Tension Crack (Excel) 30 degree joint	NO	NO	YES (Full)	Static Static	1,259	84%	Not Good	1500
		30 degree joint			[Half]	Static	1.731	115%	Good	1500
7	75	Tension Crack (Excel) 40 degree joint	ND	NO	YES (Full)	Static Static	0.879	59%	Not Good	1500
		40 degree joint			(Half)	Static	1.205	80%	Not Good	1500

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